

Utilizing Baseline Information Addition to Task-Related Information in fMRI

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Outline

1. FMRI Problem

2. FMRI Data

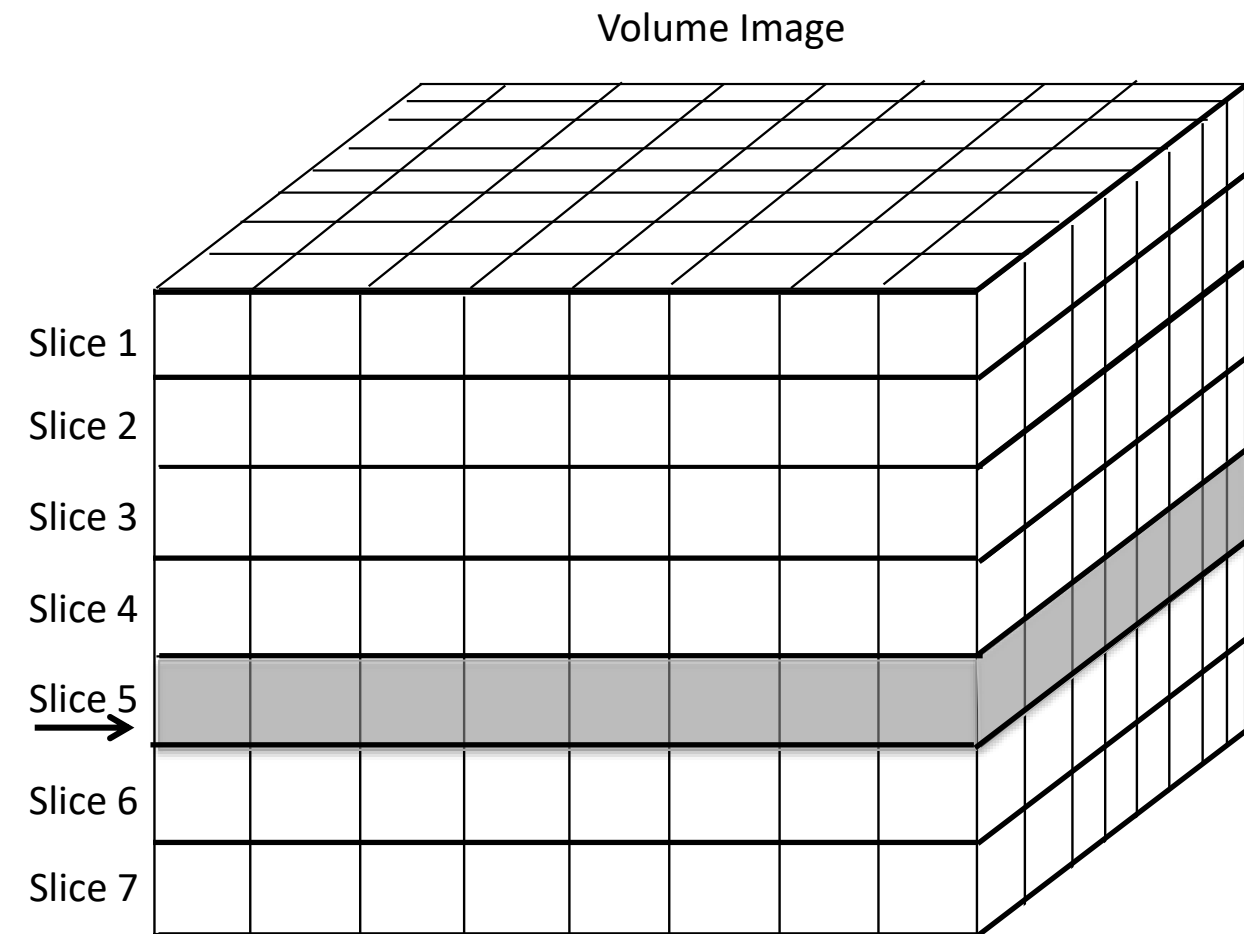
3. FMRI Activation

4. FMRI Results

5. FMRI Discussion

1. fMRI Problem

In fMRI, a subject is placed in the MRI machine and volume images of their brain measured



1. FMRI Problem

We observe $n(=490)$, data points, $(x_1, y_1), \dots, (x_n, y_n)$ and determine a statistically significant relationship between x (task design) and y (observed voxel value) as $y_t = \beta_0 + \beta_1 x_t + \varepsilon_t$, assuming $\varepsilon_t \sim N(0, \sigma^2)$ for $t=1, \dots, n$.

In each voxel

$$W = (X'X)^{-1}$$

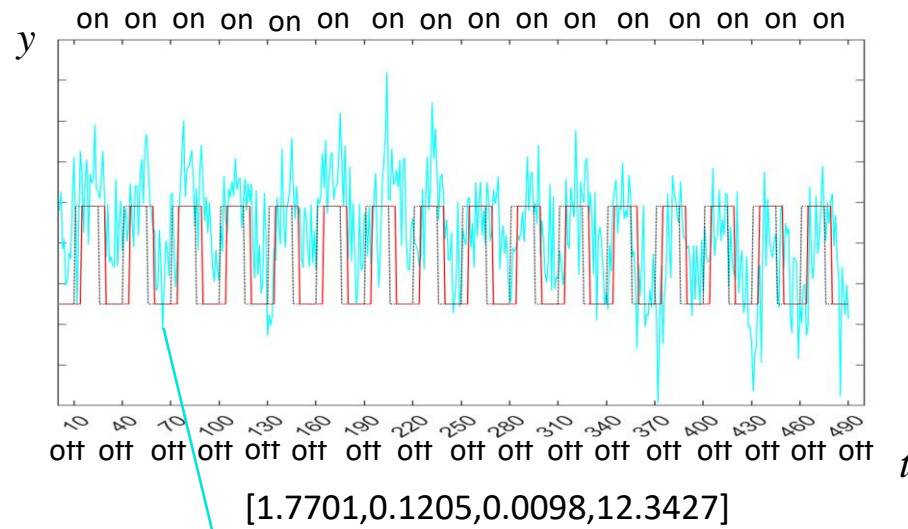
$$W = \begin{pmatrix} w_{11} & w_{12} \\ w_{21} & w_{22} \end{pmatrix}$$

$$SE(\hat{\beta}_1) = s \sqrt{w_{22}}$$

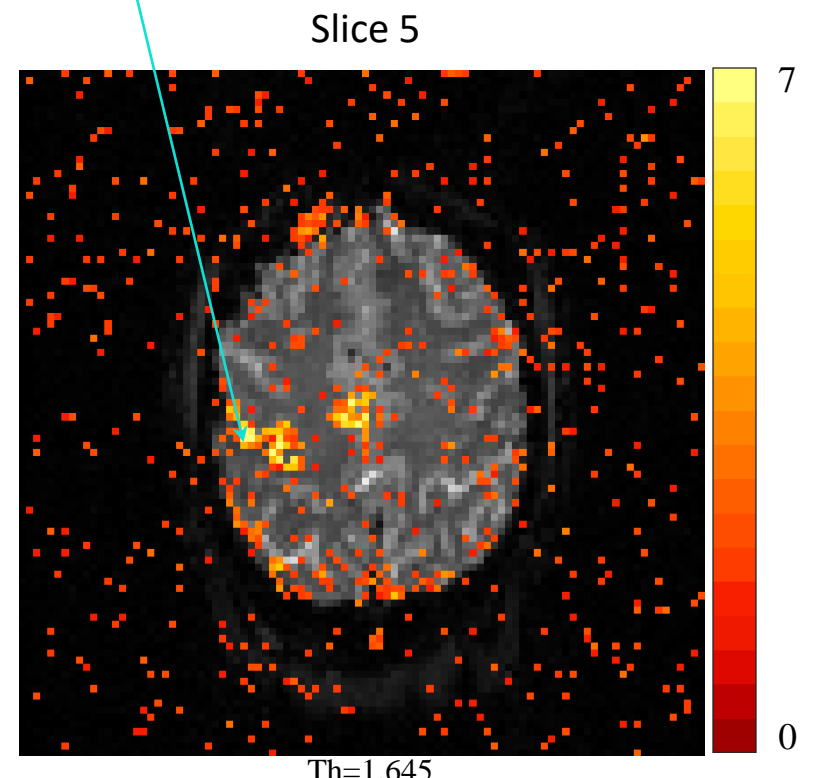
$$\hat{\beta} = (X'X)^{-1} X'y$$

$$t = \frac{\hat{\beta}_1}{SE(\hat{\beta}_1)} \longrightarrow$$

As you can see there are many "false positives."

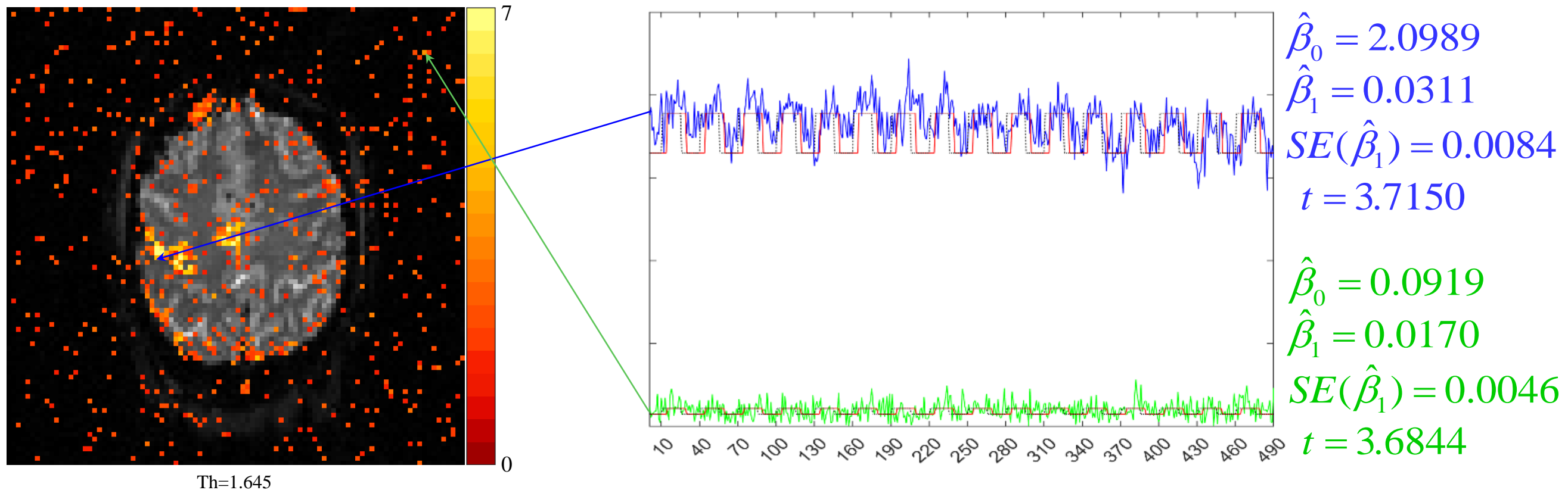


[1.7701, 0.1205, 0.0098, 12.3427]



1. FMRI Problem

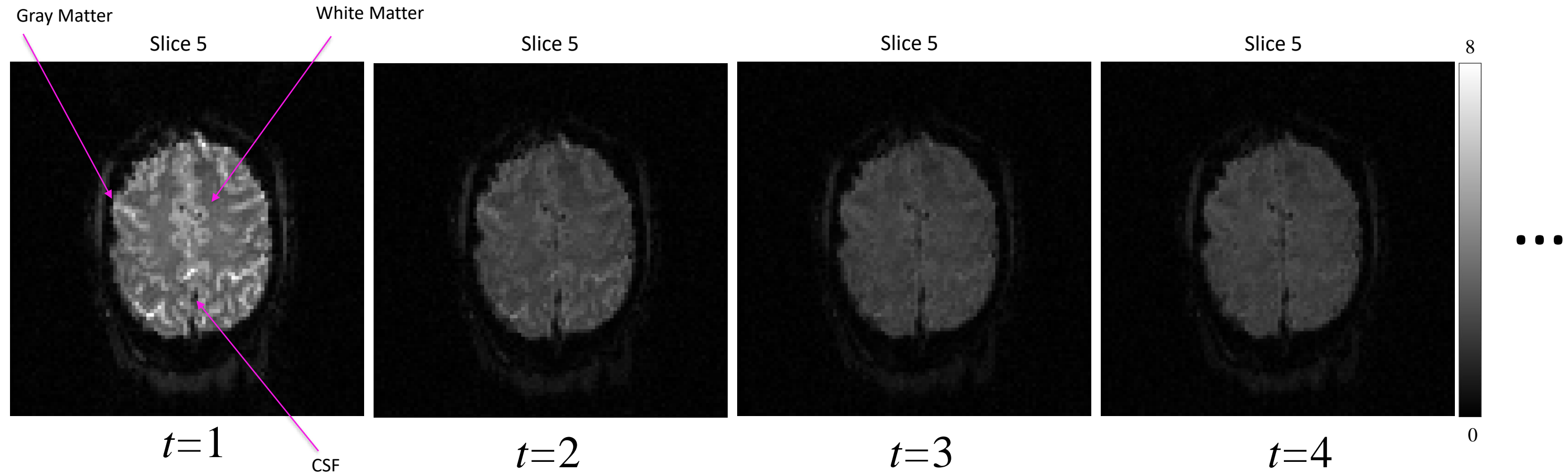
The issue is that we can have two voxels that have the same β_1 “activation” level, but different baselines, β_0 .



We don't use the β_0 information that we have.

2. FMRI Data

For FMRI Data, these are what the slice images look like over time.

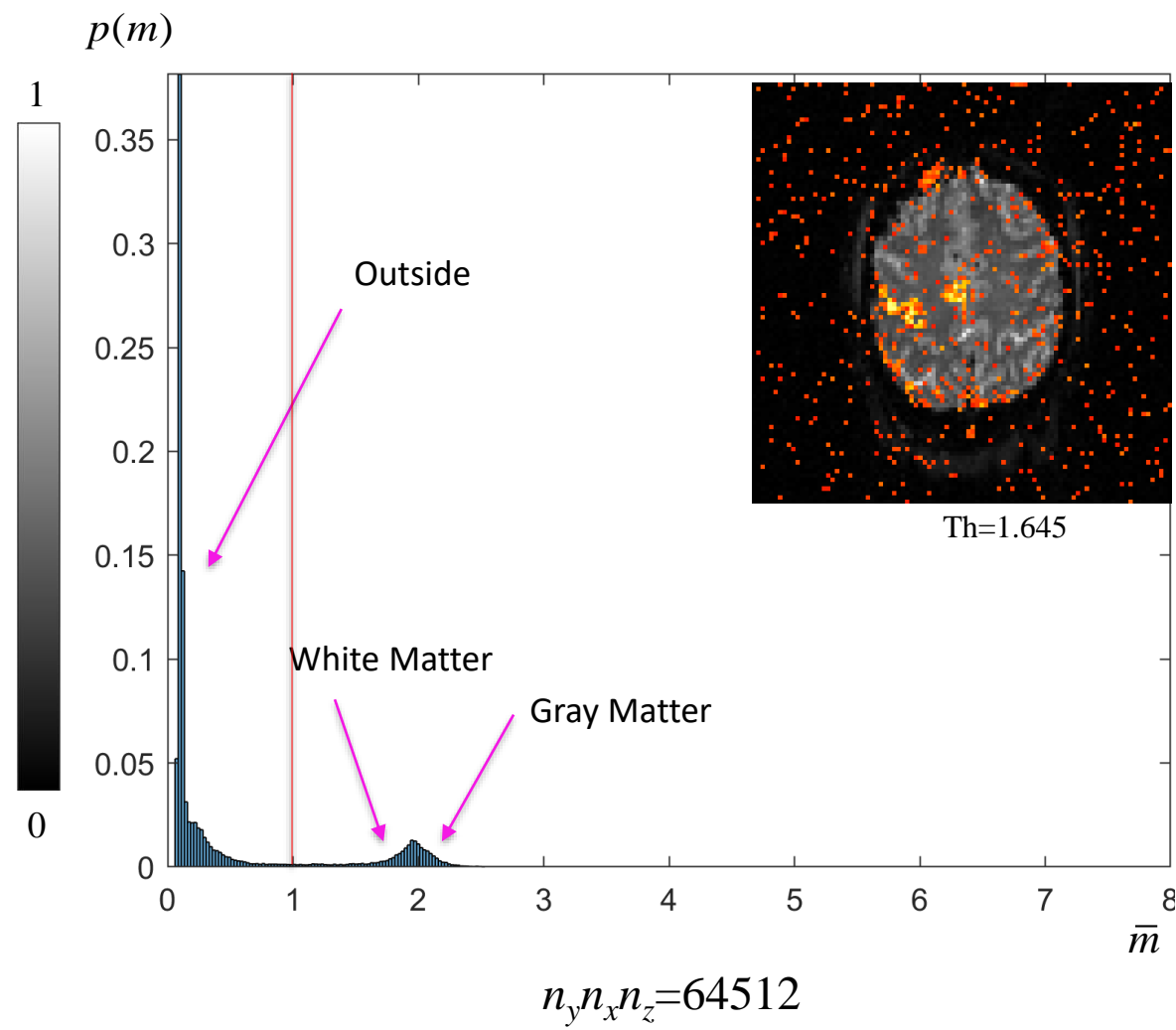
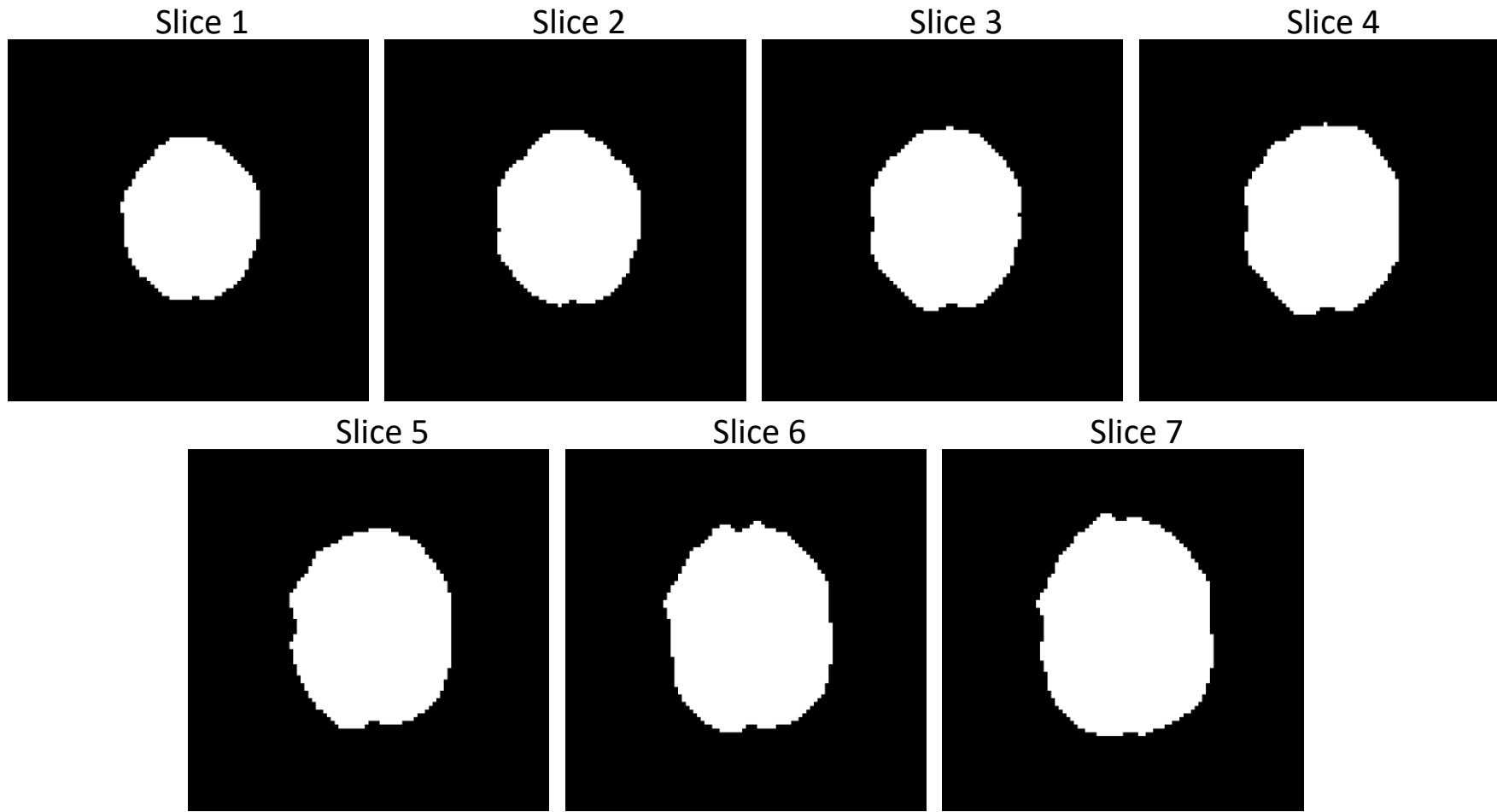


T_2^* weighted images

Signal equilibration effect. Most never see these after “preprocessing.”

2. FMRI Data

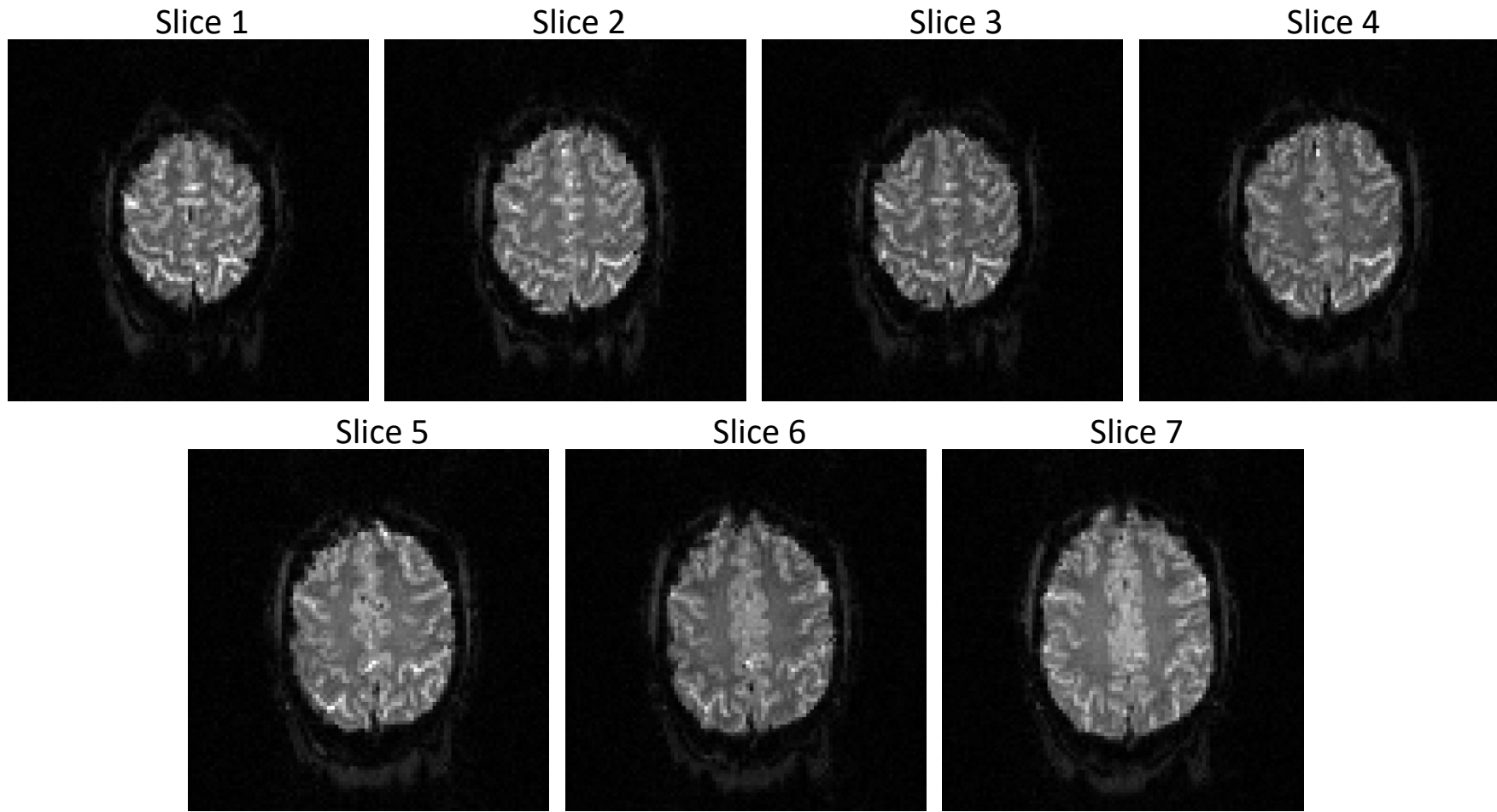
For FMRI Data, a spatial mask based upon intensity can be generated.



1. Averaged n_{del}^+, \dots, n images.
2. Smoothed with 5×5 mean filter.
3. Pixel intensities > 1 in mask.

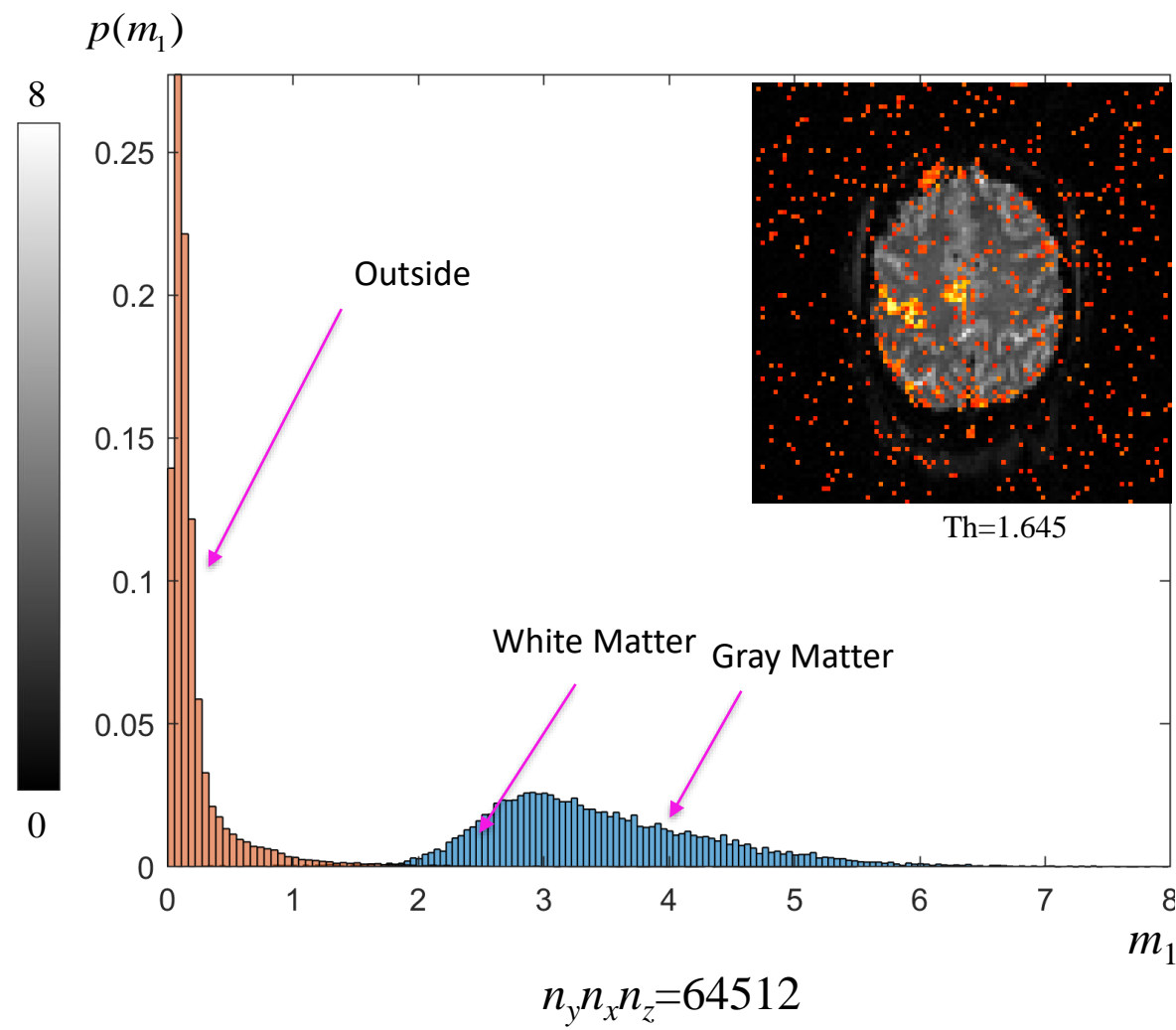
2. FMRI Data

For FMRI Data, these are what the first time point slice images look like.



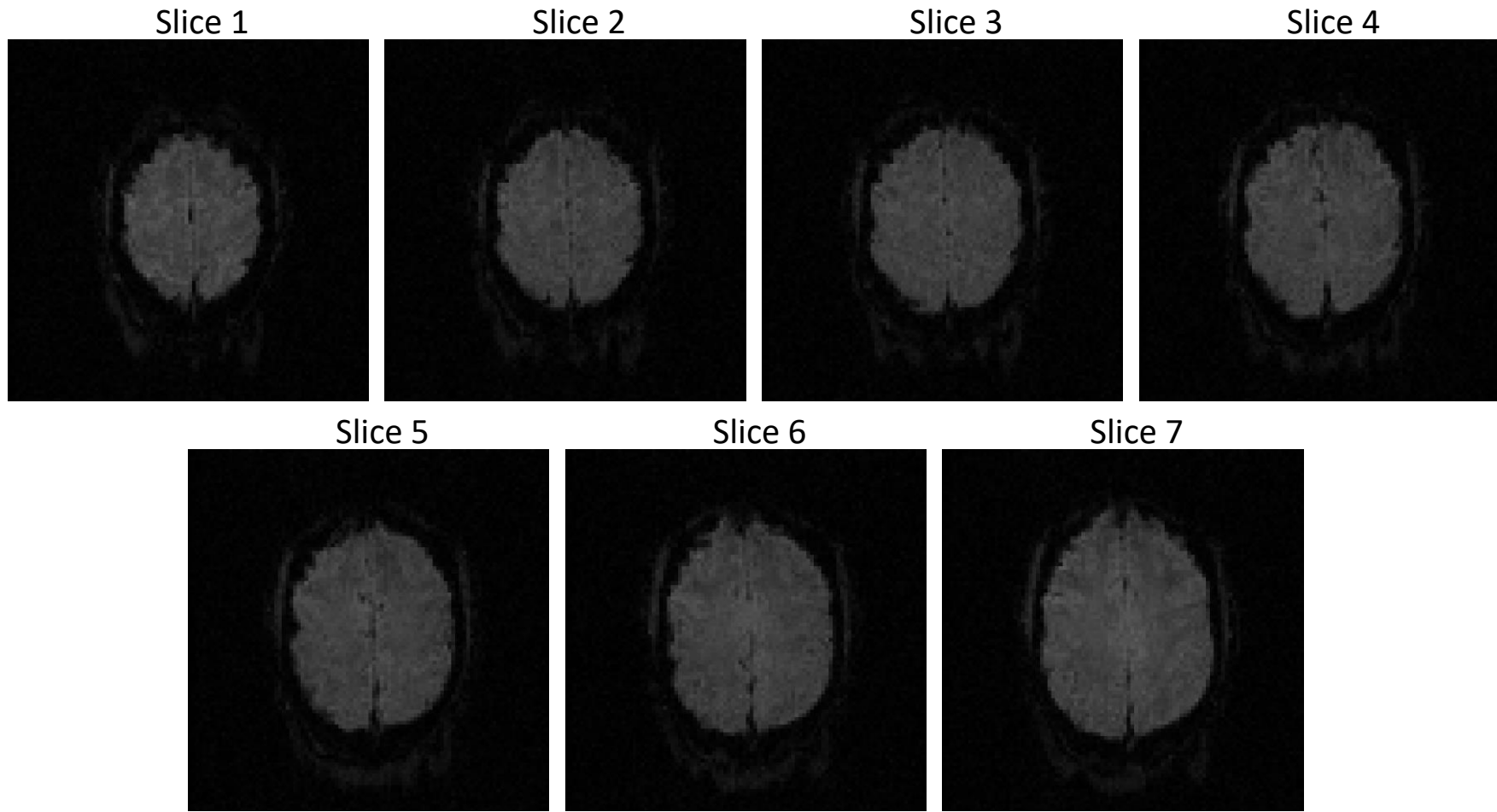
Usually Discarded $t=1$

T_2^* weighted images



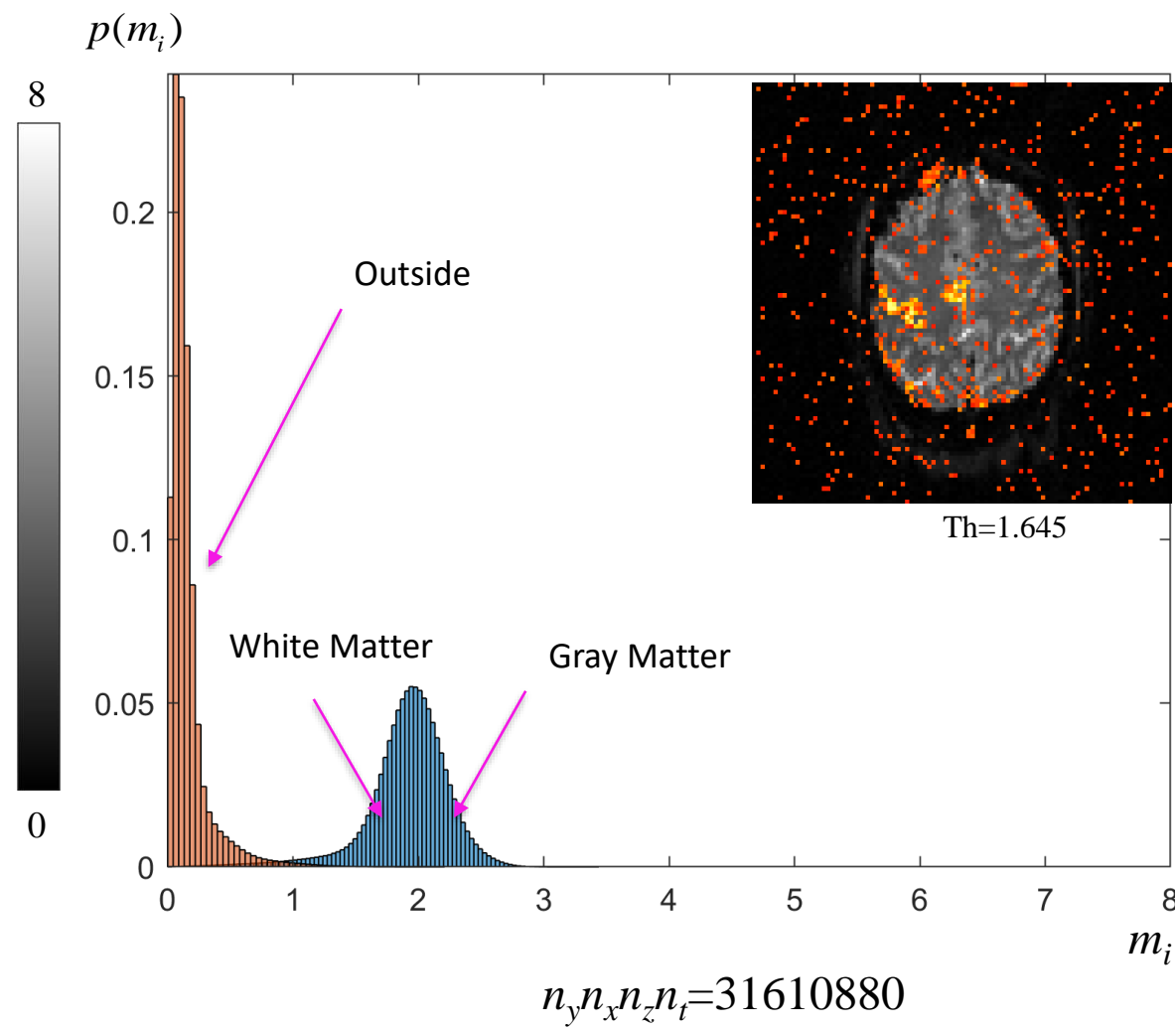
2. FMRI Data

For FMRI Data, these are what the after discarded slice images look like.



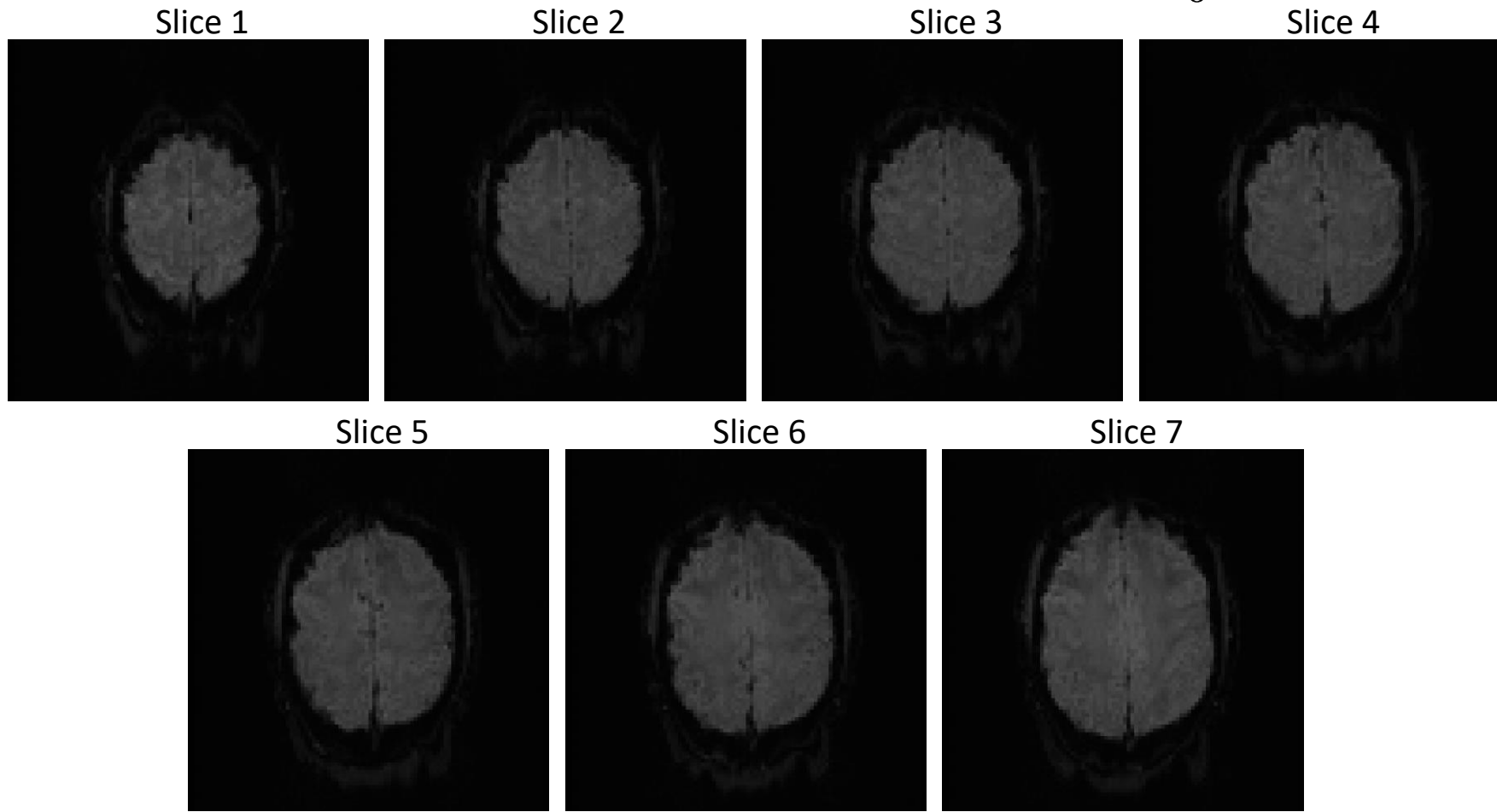
$$t = n_{del} + 1, \dots, n$$

T_2^* weighted images



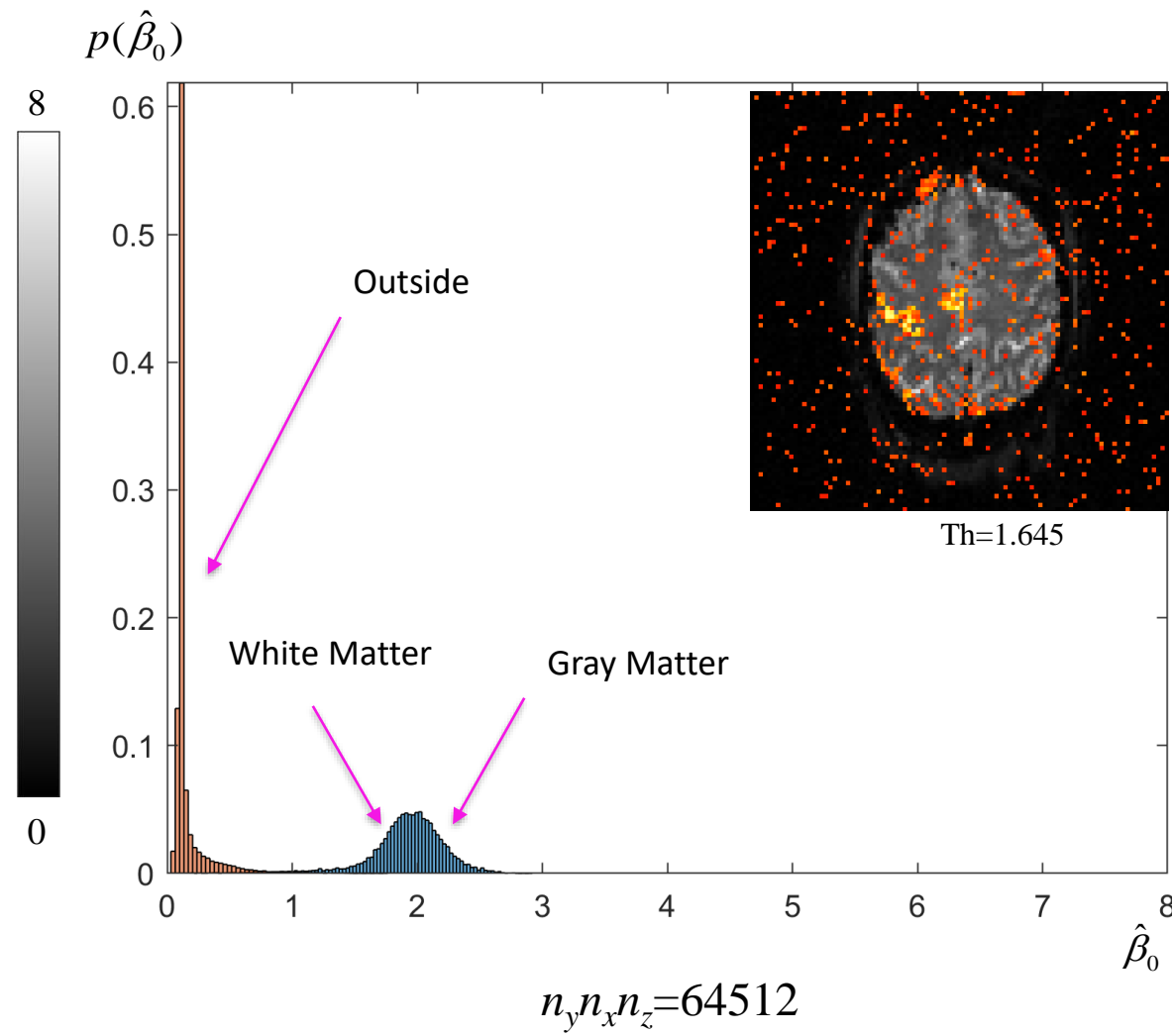
2. FMRI Data

For FMRI Data, these are what the β_0 coefficients look like.



$$t = n_{del} + 1, \dots, n$$

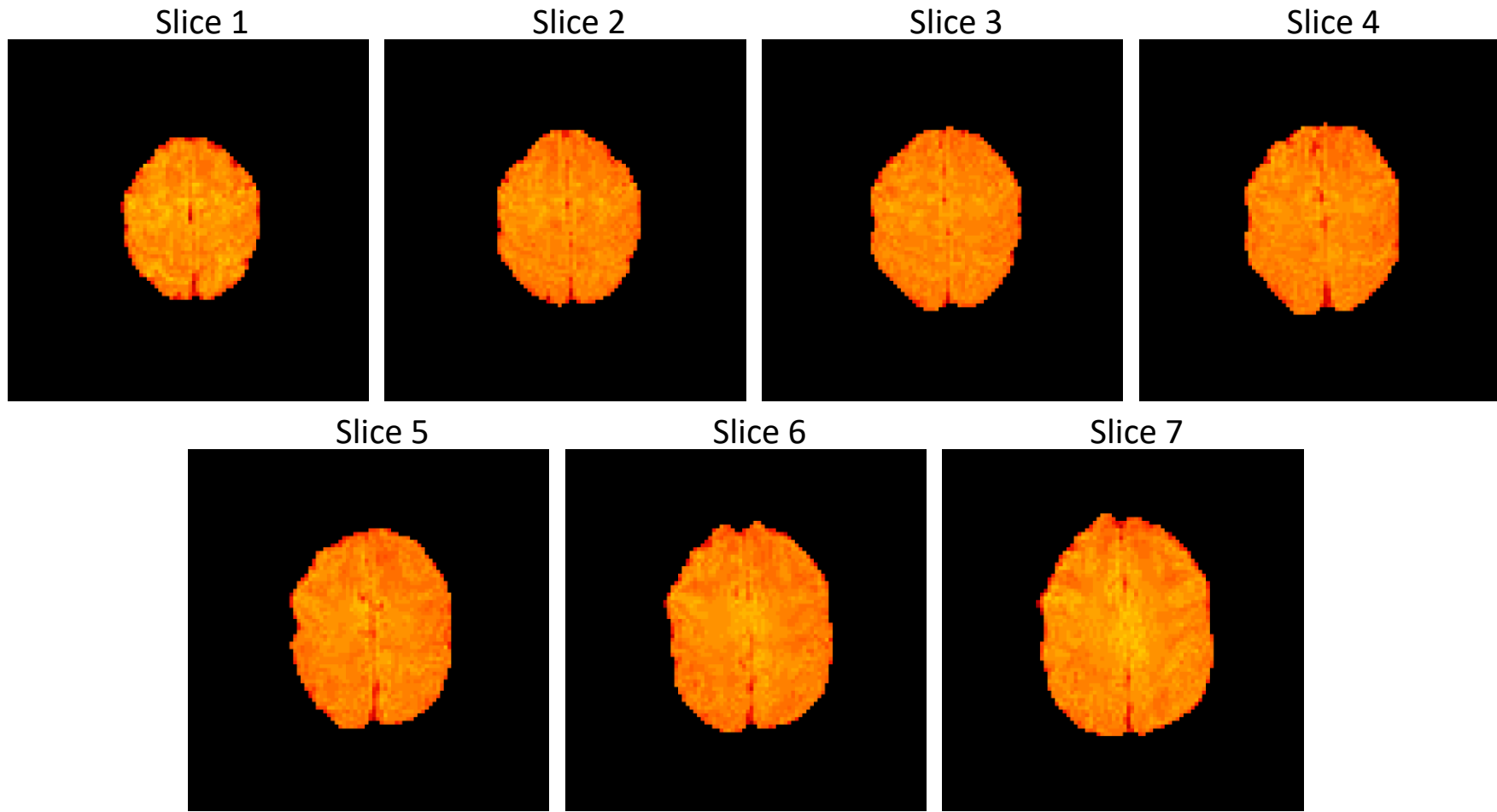
T_2^* weighted images



3. FMRI Activation

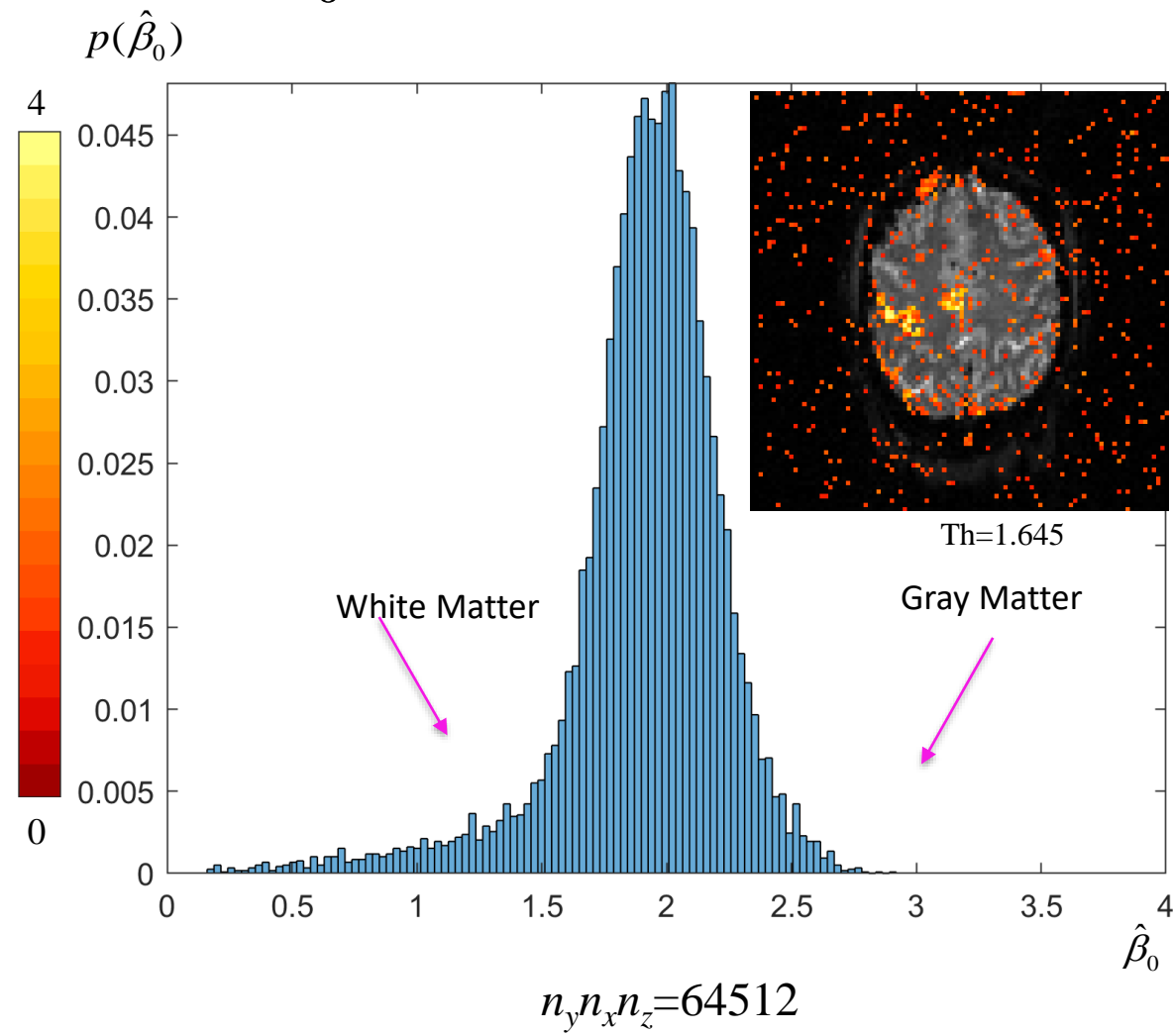
$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

For FMRI Data, we can limit ourselves to within mask β_0 voxels.



$$t = n_{del} + 1, \dots, n$$

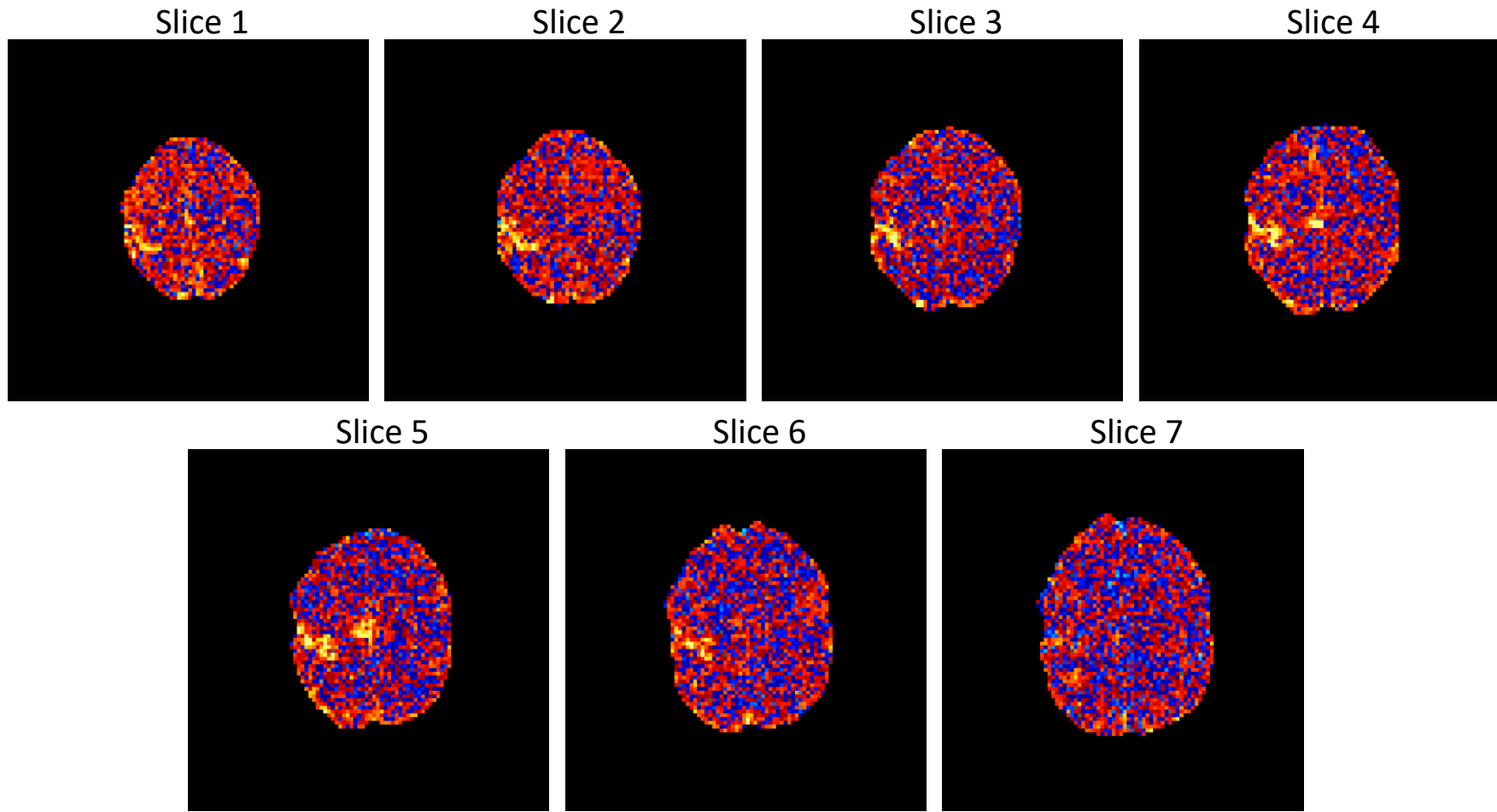
T_2^* weighted images



3. FMRI Activation

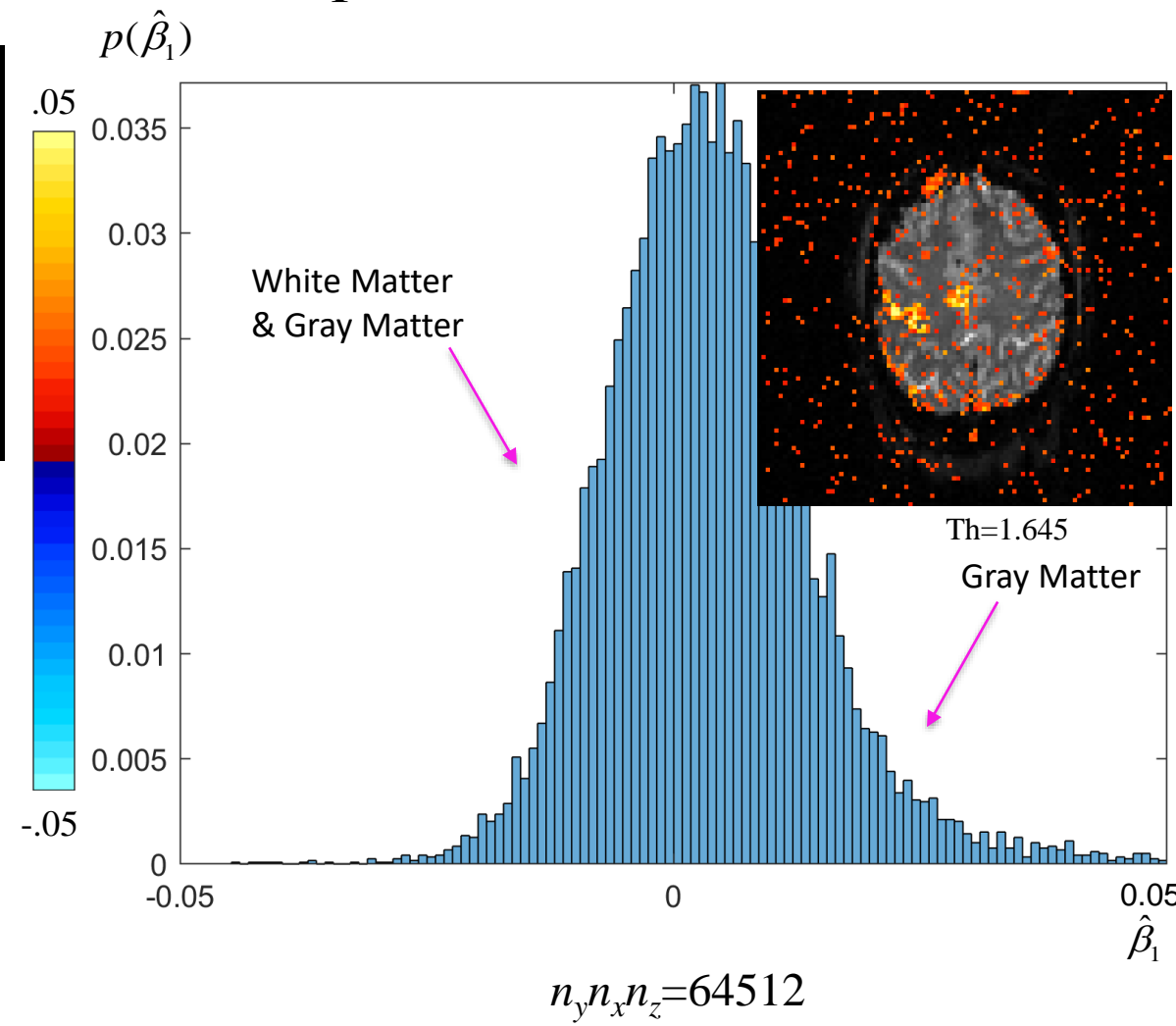
$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

For FMRI Data, we can limit ourselves to within mask β_1 voxels.



$$t = n_{del} + 1, \dots, n$$

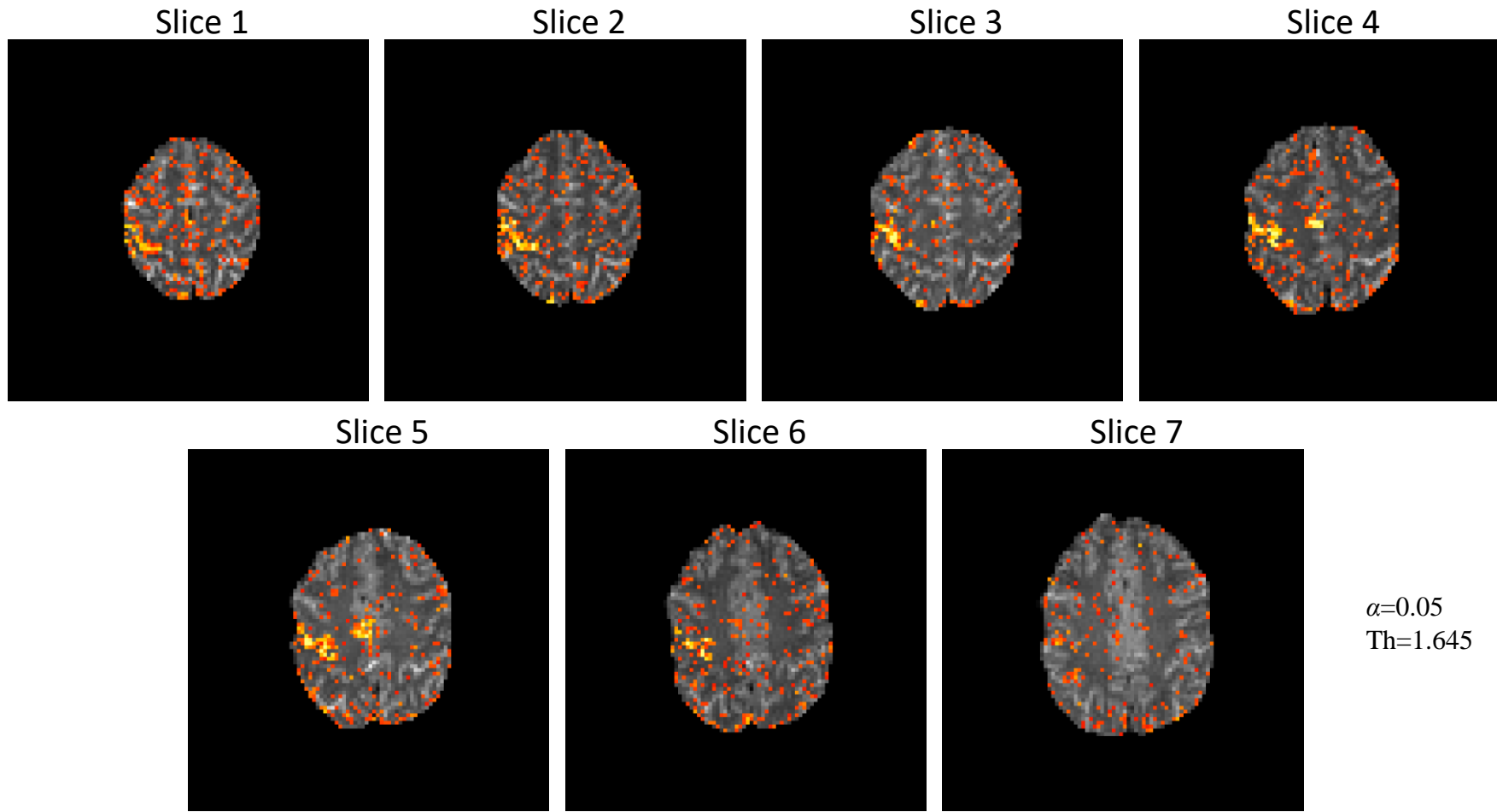
T_2^* weighted images



3. FMRI Activation

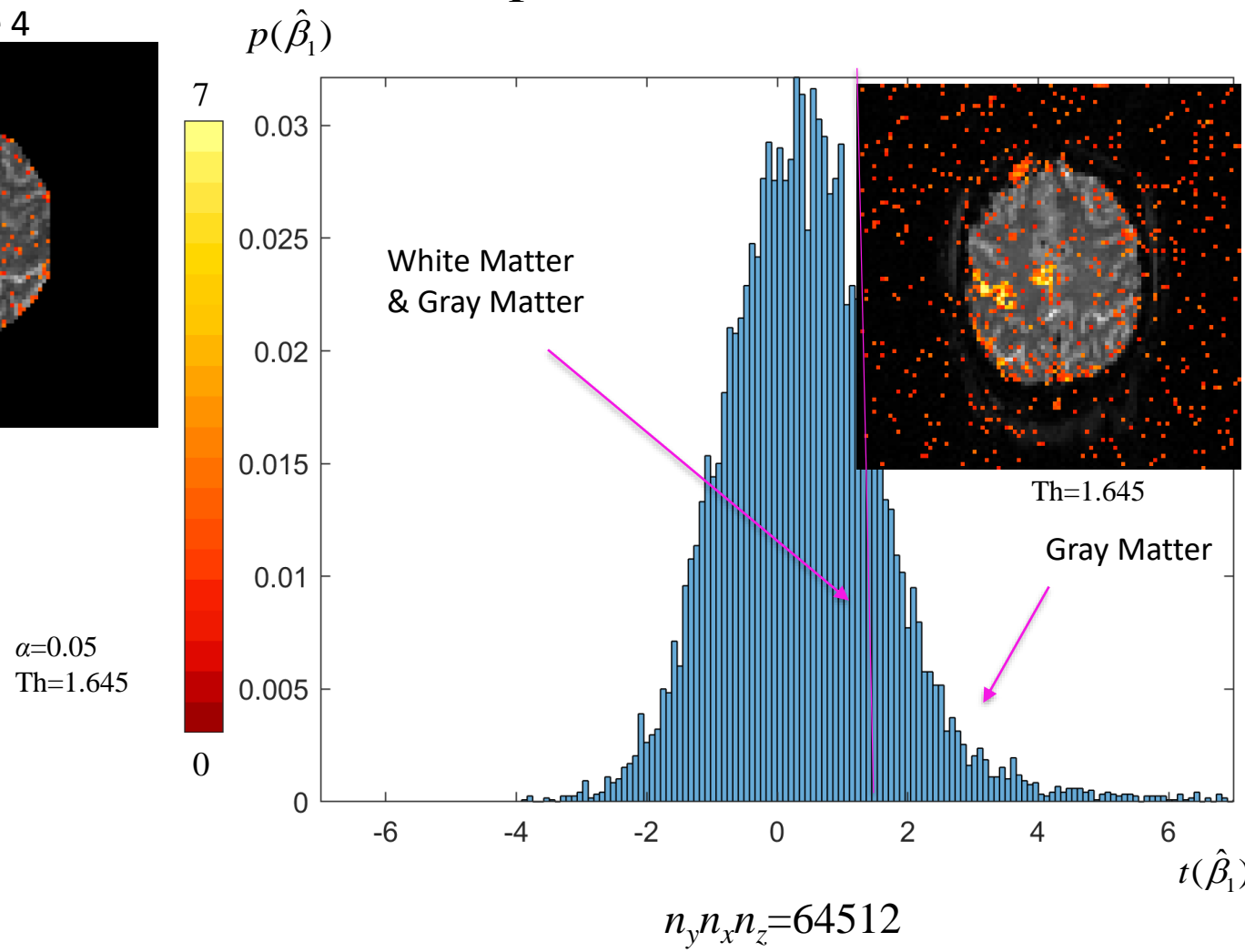
$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

For FMRI Data, we can limit ourselves to within mask $t(\beta_1)$ voxels.



$$t = n_{del} + 1, \dots, n$$

T_2^* weighted images



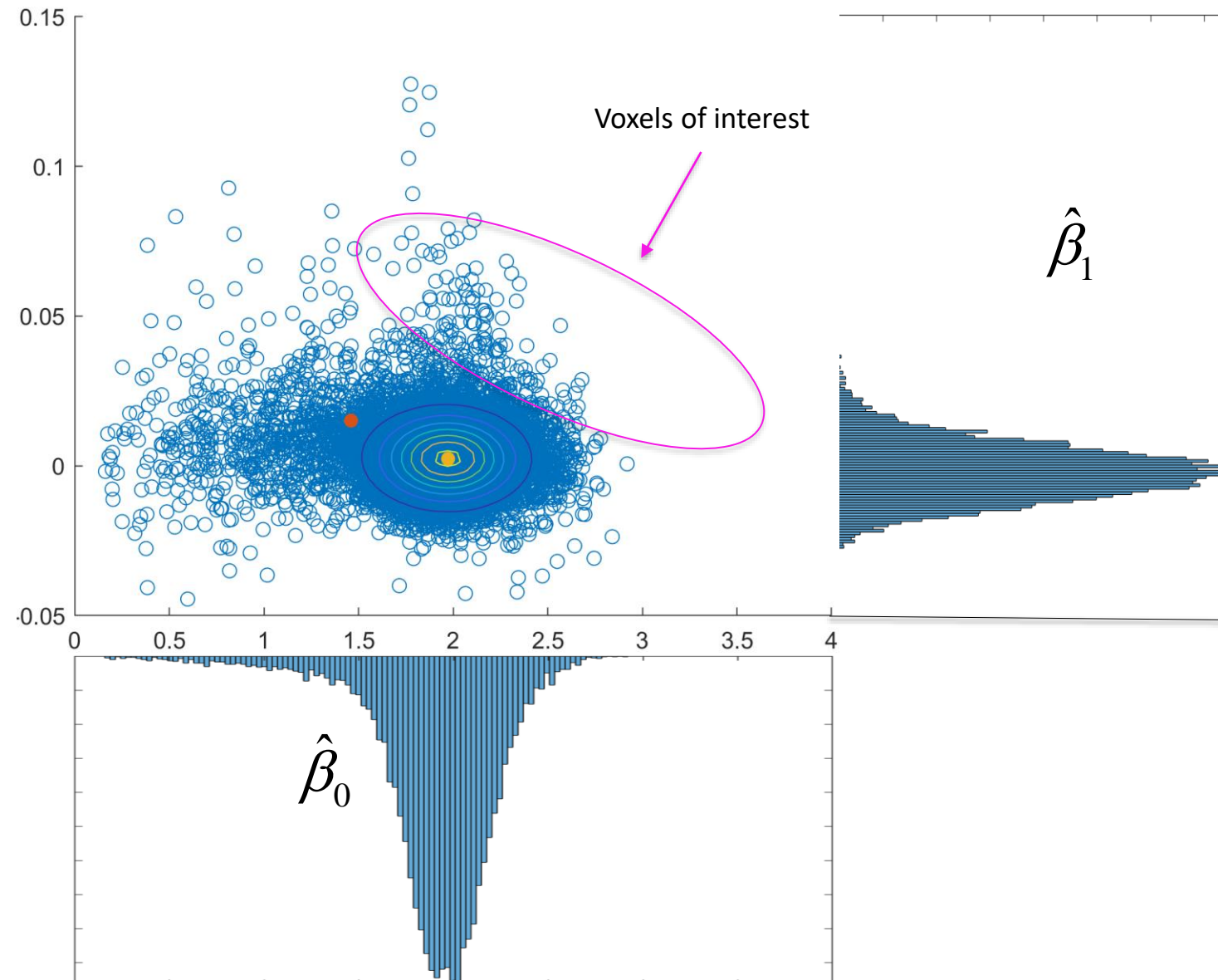
$\alpha=0.05$
 $Th=1.645$

$n_y n_x n_z = 64512$

3. FMRI Activation

$$y_t = \beta_0 + \beta_1 x_t + \varepsilon_t$$

For FMRI Data, we can plot within mask β_0 and β_1 coefficients.



Fit a 2 population bivariate Normal Mixture model.

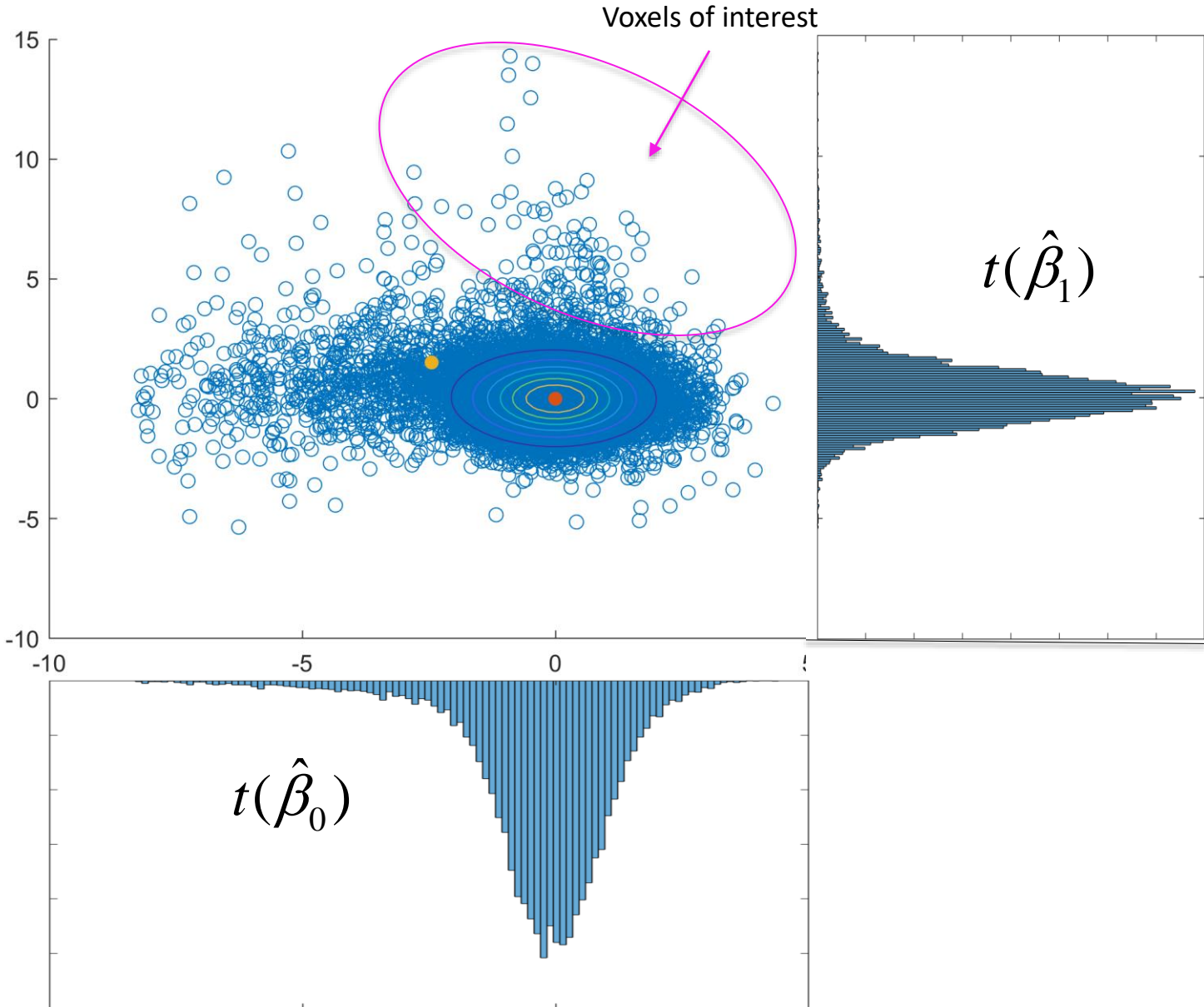
$$\mu_1 = \begin{bmatrix} 1.4611 \\ 0.0151 \end{bmatrix} \quad \Sigma_1 = \begin{bmatrix} 0.2834 & 0.0026 \\ 0.0026 & 0.0004 \end{bmatrix}$$

$$\mu_2 = \begin{bmatrix} 1.9735 \\ 0.0024 \end{bmatrix} \quad \Sigma_2 = \begin{bmatrix} 0.0484 & 0.0000 \\ 0.0000 & 0.0001 \end{bmatrix}$$

3. FMRI Activation

$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

For FMRI Data, we can plot within mask $t(\beta_0)$ and $t(\beta_1)$ coefficients.



Fit a 2 population bivariate Normal Mixture model.

$$\mu_1 = \begin{bmatrix} -2.3245 \\ 1.4548 \end{bmatrix} \quad \Sigma_1 = \begin{bmatrix} 5.8613 & 1.3268 \\ 1.3268 & 5.4182 \end{bmatrix}$$

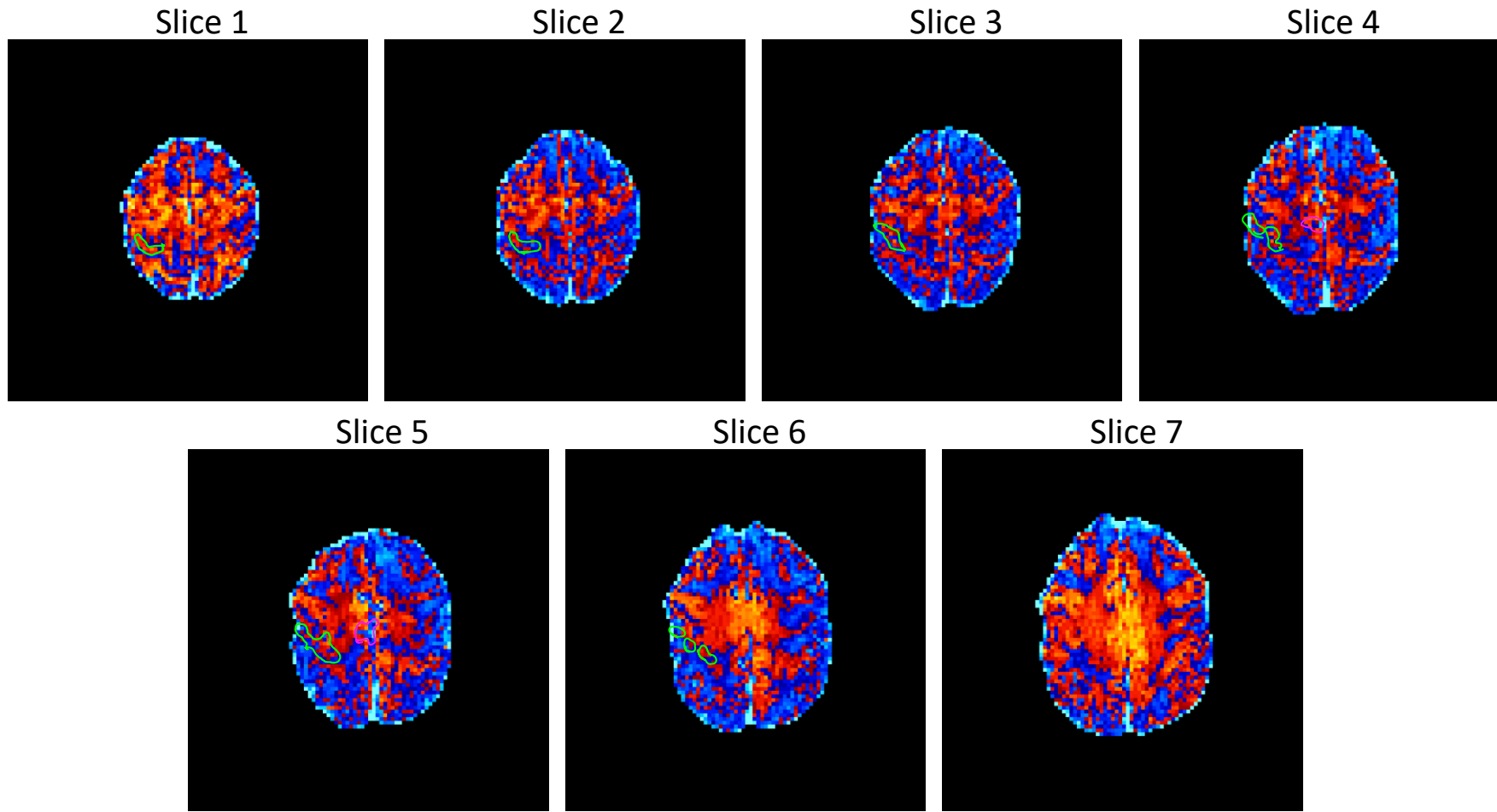
$$\mu_2 = \begin{bmatrix} 0.0000 \\ -0.0001 \end{bmatrix} \quad \Sigma_2 = \begin{bmatrix} 0.9995 & -0.0076 \\ -0.0076 & 0.9996 \end{bmatrix}$$

Formed t-statistics using main fitted PDF.

3. FMRI Activation

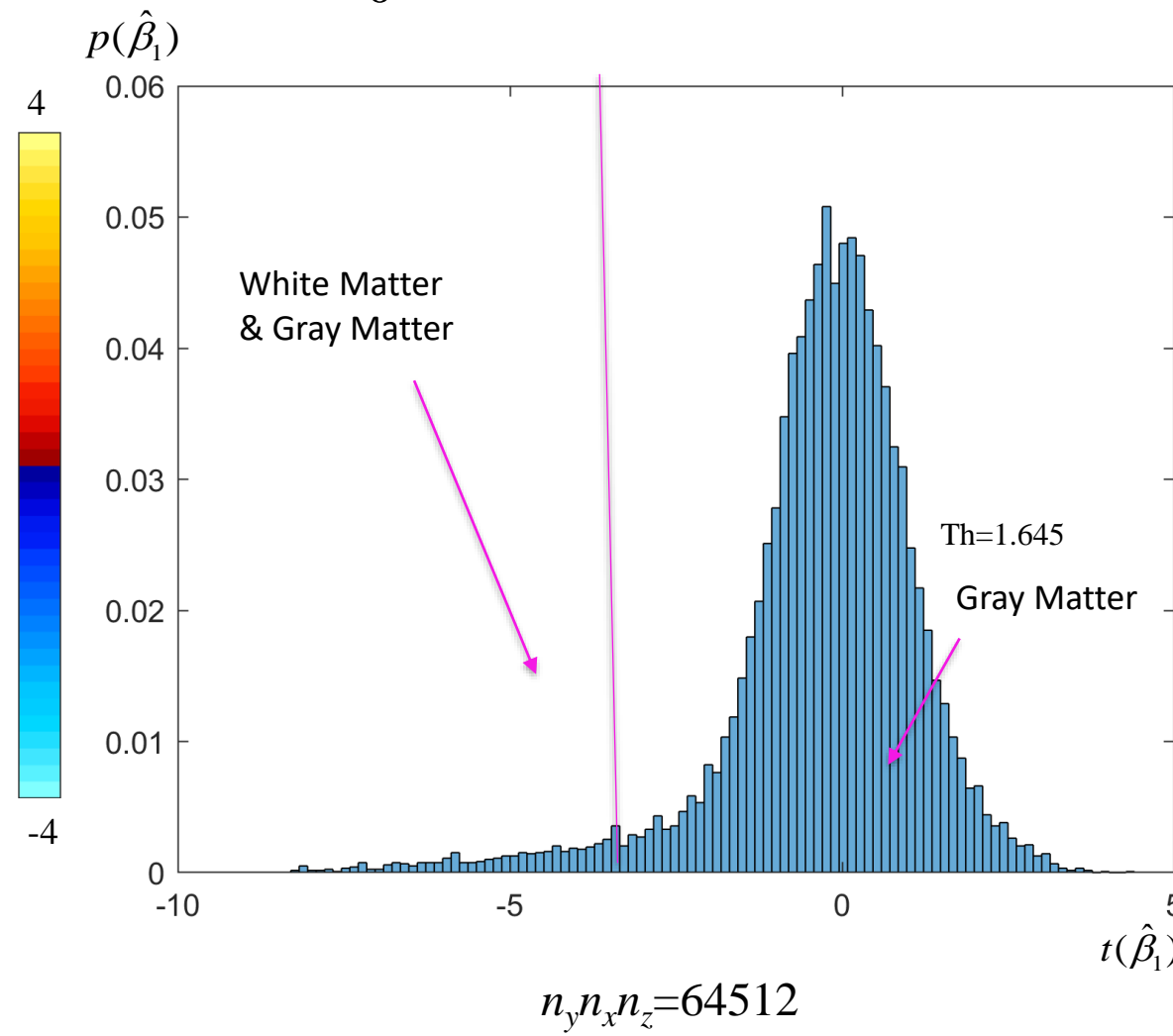
$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

For FMRI Data, we can limit ourselves to within mask $t(\beta_0)$ voxels.



$$t = n_{del} + 1, \dots, n$$

T_2^* weighted images

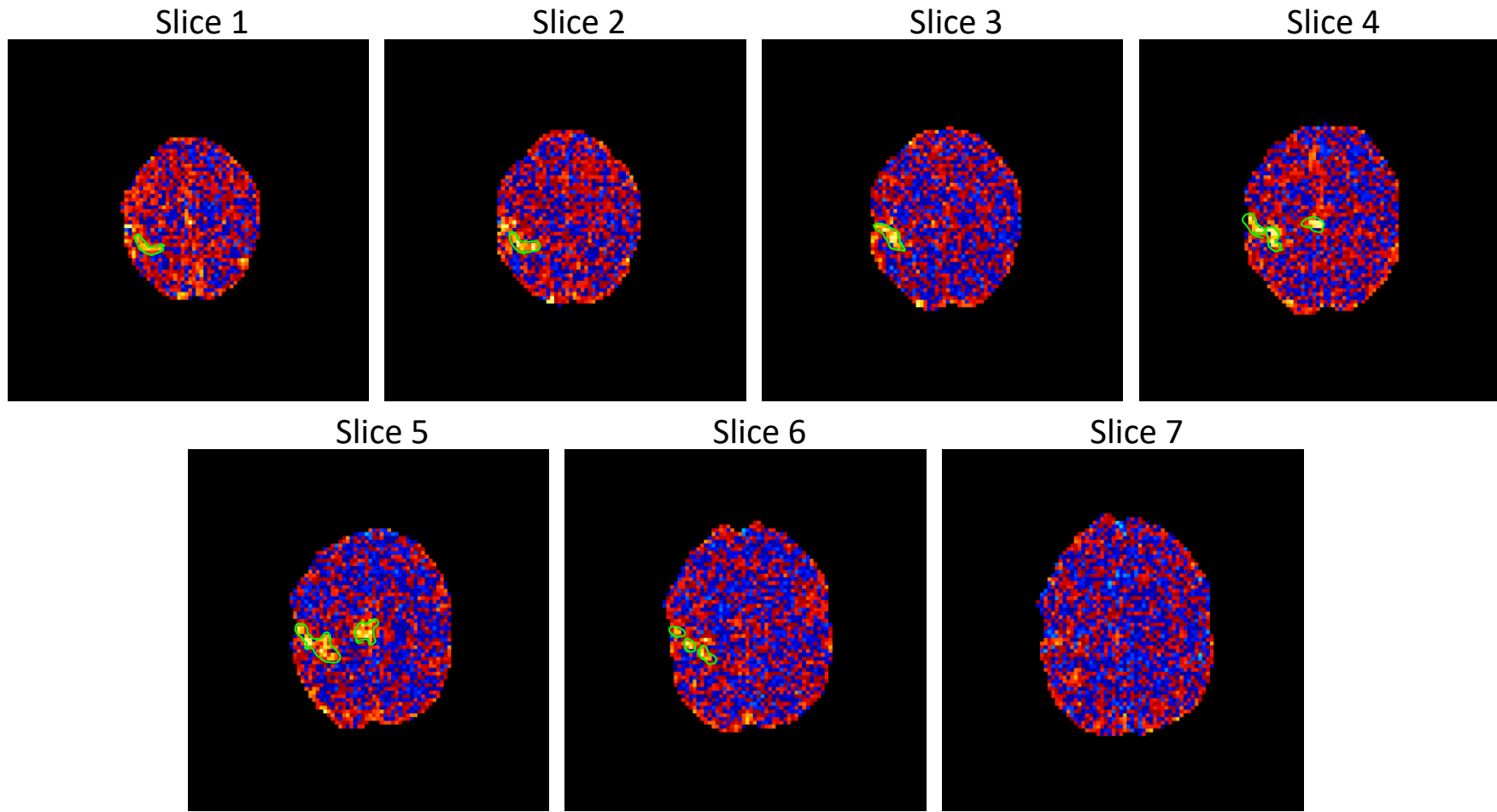


$n_y n_x n_z = 64512$

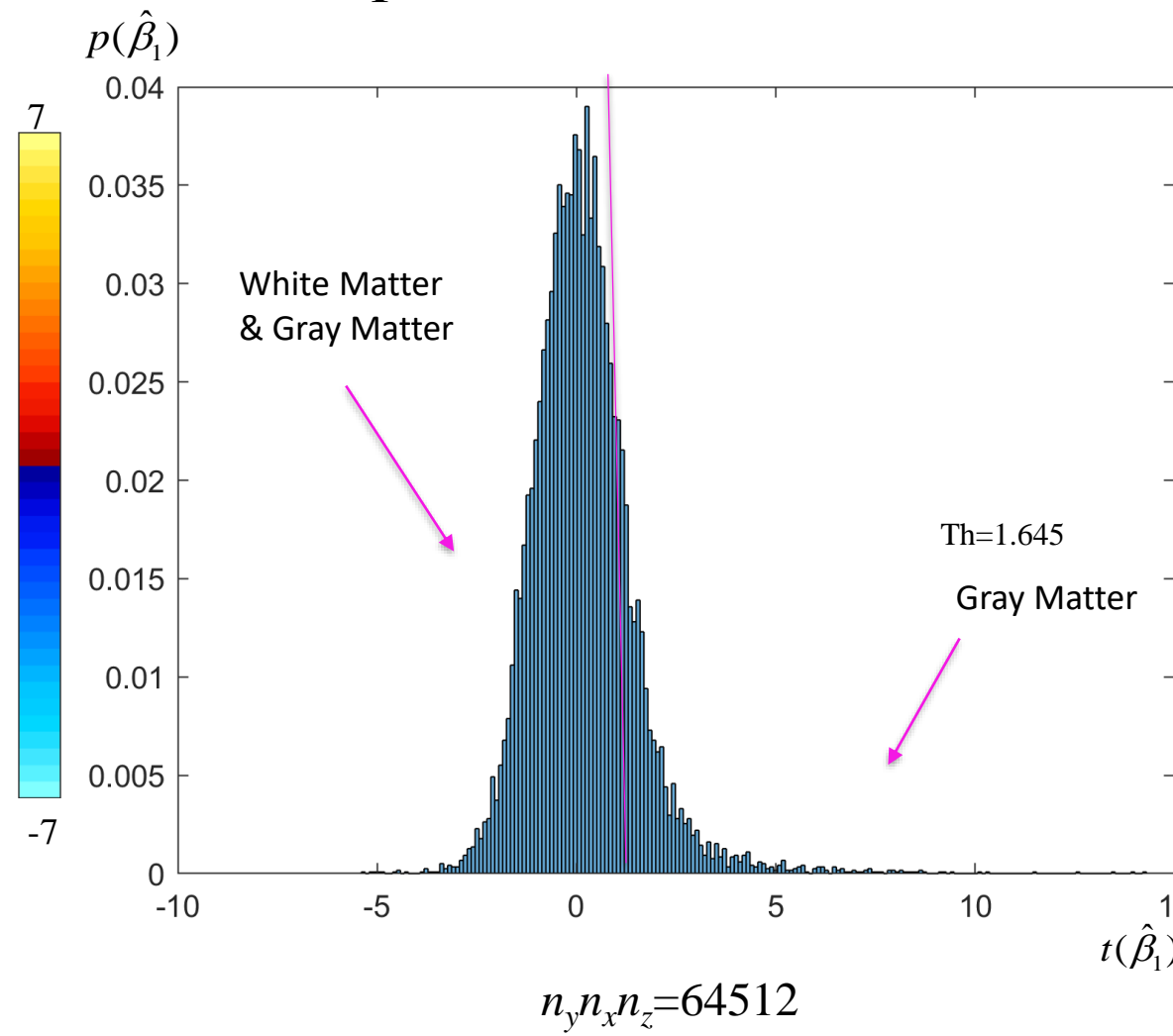
3. FMRI Activation

$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

For FMRI Data, we can limit ourselves to within mask $t(\beta_1)$ voxels.



$$t = n_{del} + 1, \dots, n$$

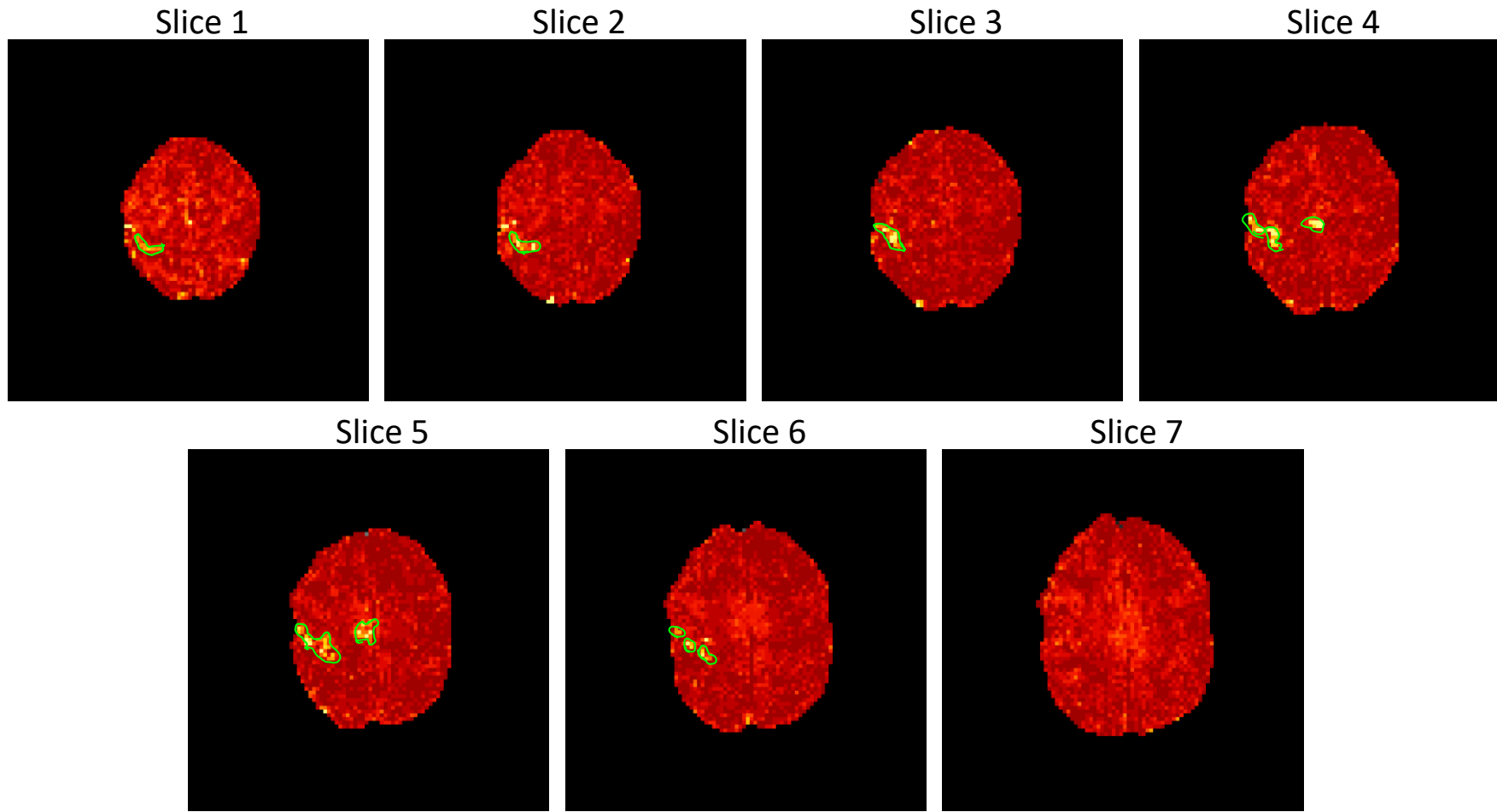


T_2^* weighted images

4. FMRI Results

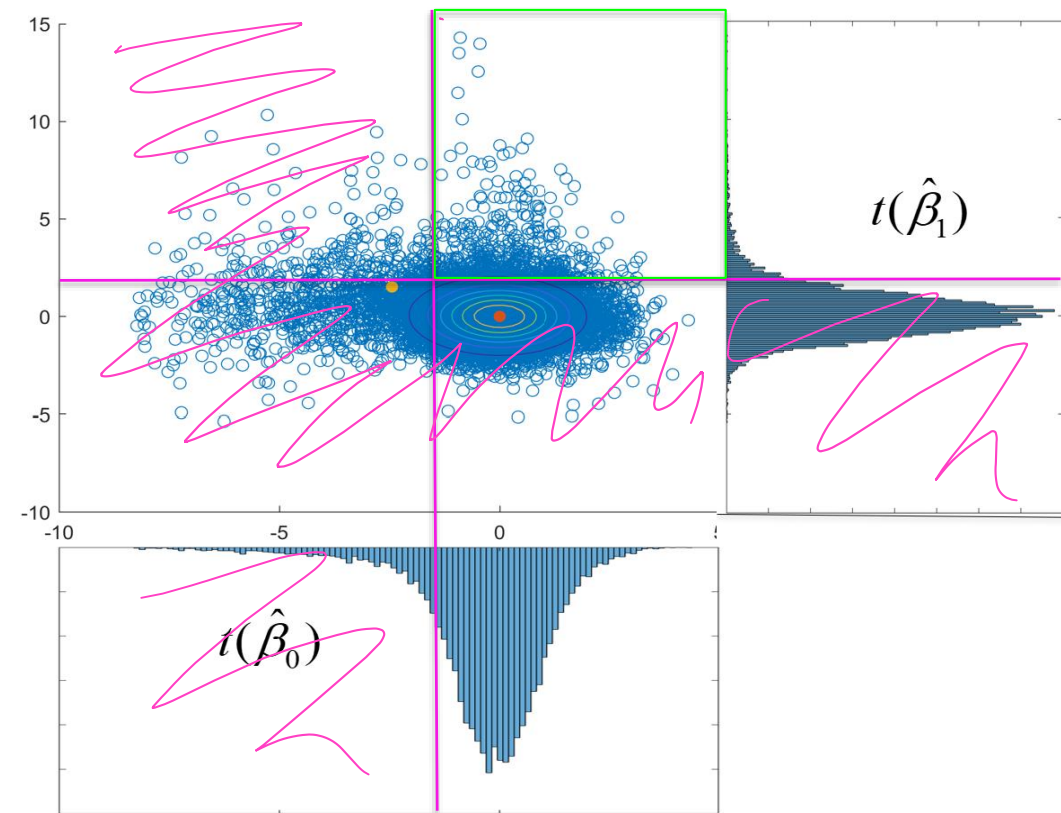
$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

We can multiply p -values together and display $-\log_{10}(p\text{-value})$.



$$t = n_{del} + 1, \dots, n$$

T_2^* weighted images

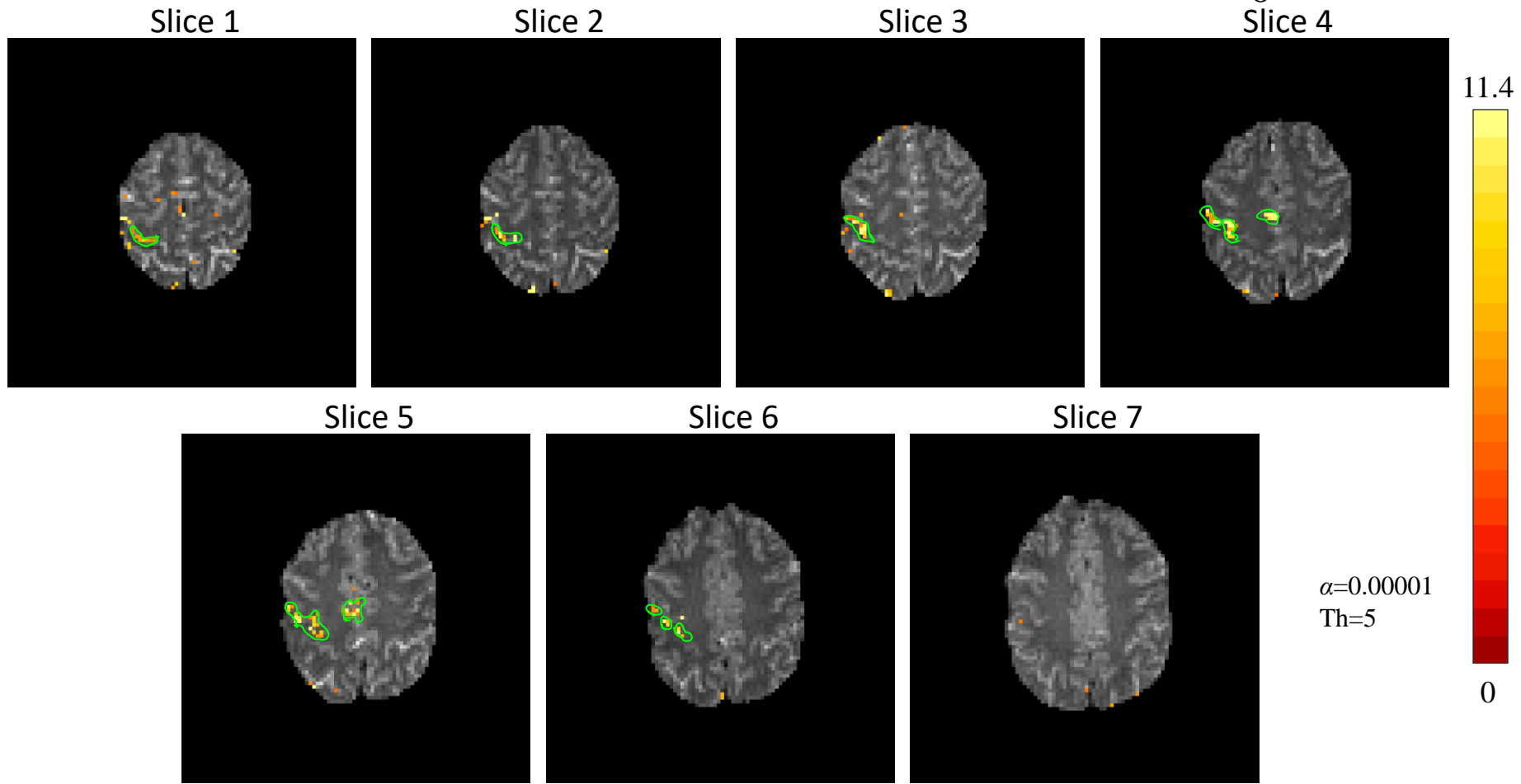


Multipled of β_0 and of β_1 p -values together.

4. FMRI Results

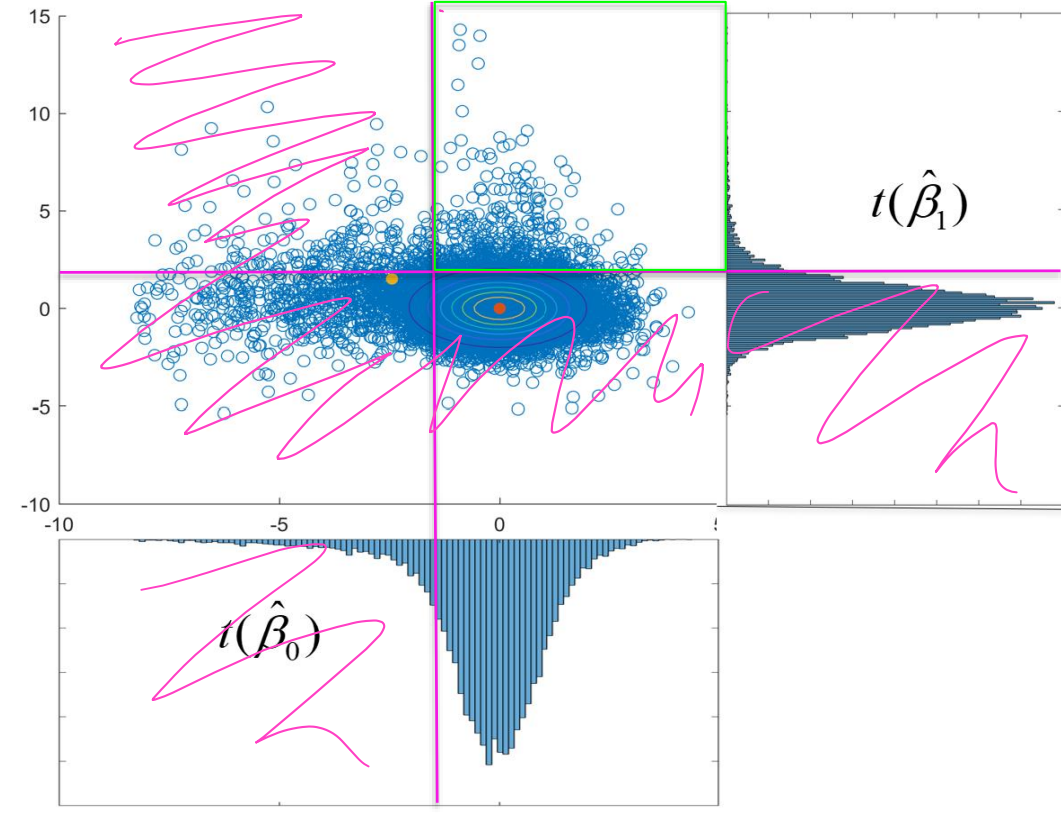
$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

We can eliminate lower probability of $t(\beta_0)$ and of $t(\beta_1)$.



$$t = n_{del} + 1, \dots, n$$

T_2^* weighted images

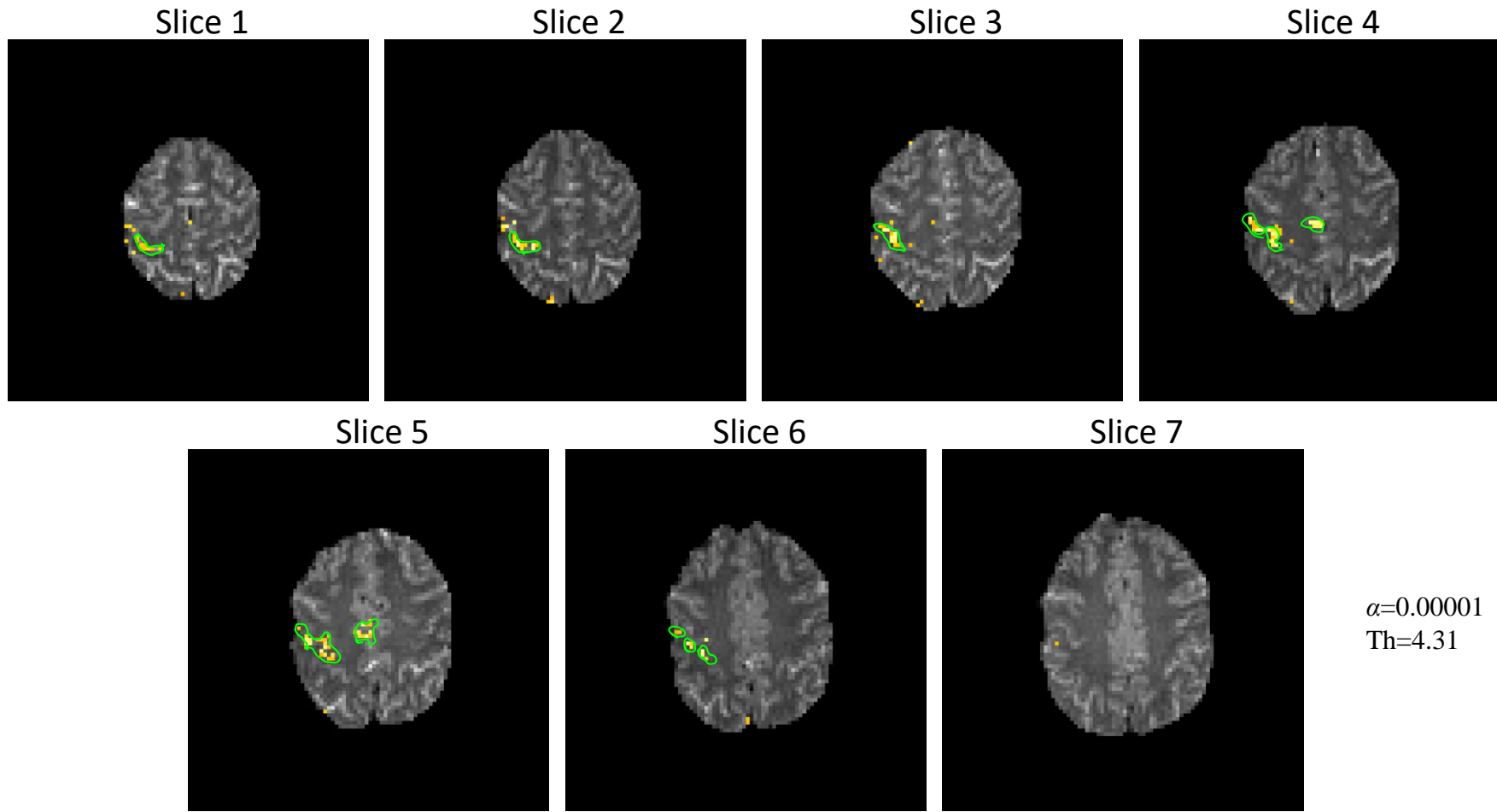


Multipled of β_0 and of β_1 p -values together.

3. FMRI Activation

$$y_t = \beta_0 + \beta_1 x_t + \epsilon_t$$

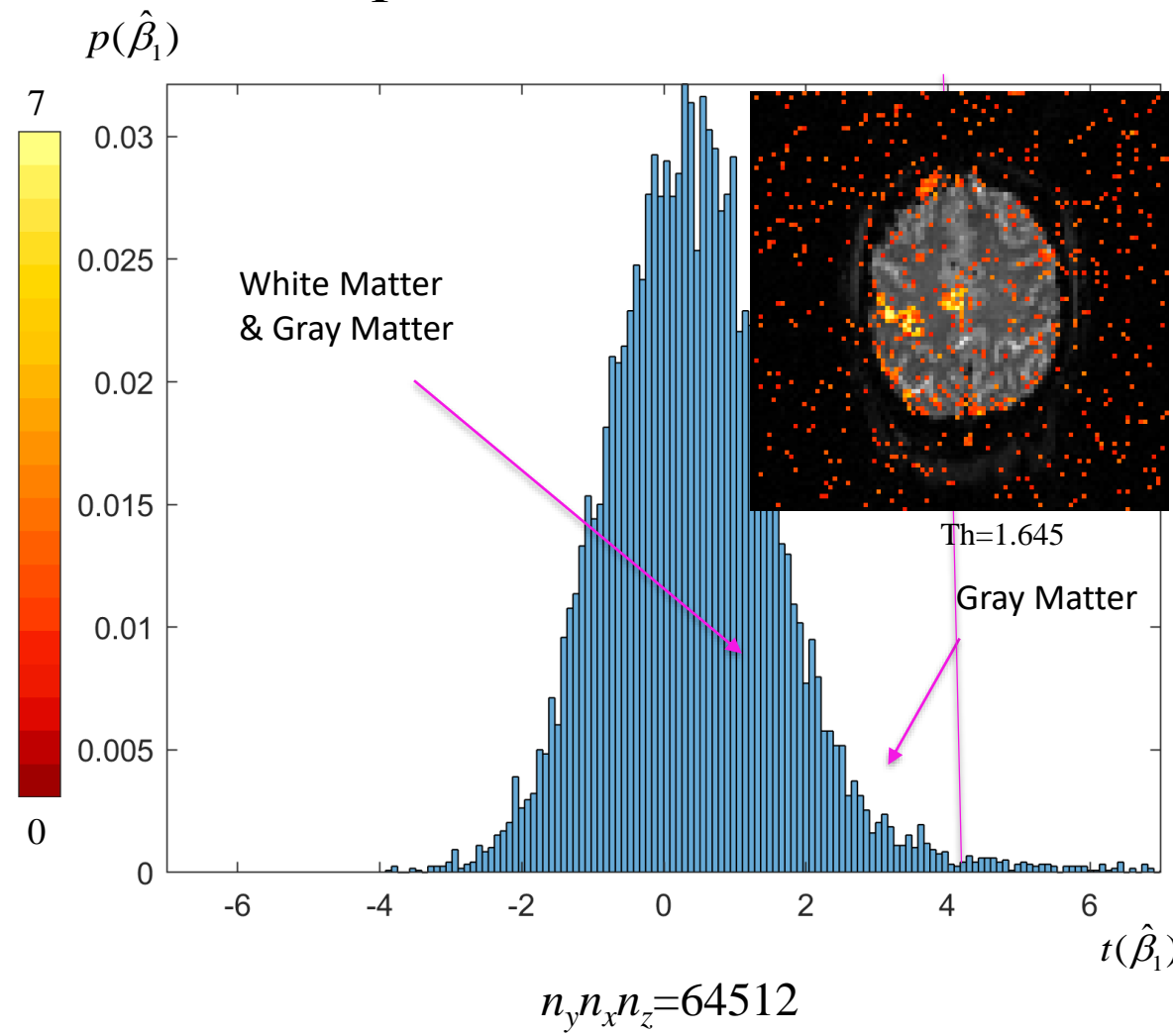
For FMRI Data, we can limit ourselves to within mask $t(\beta_1)$ voxels.



$$t = n_{del} + 1, \dots, n$$

T_2^* weighted images

$\alpha = 0.00001$
 $Th = 4.31$



5. Discussion

Presented usual fMRI process with t-statistics of β_1 .

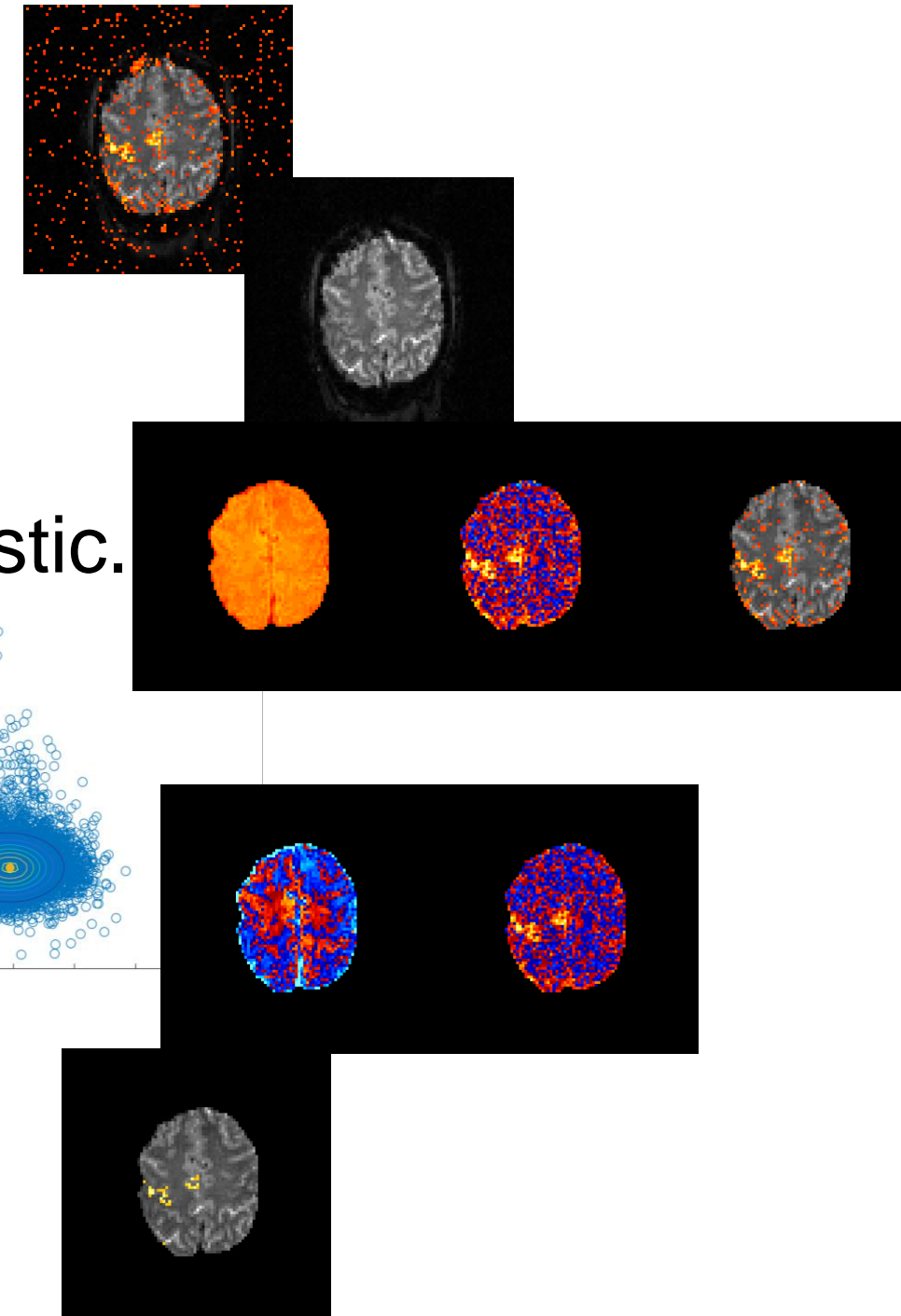
Presented usually discarded first images data.

Presented of β_0 and of β_1 coefficients and of β_1 t-statistic.

Presented bivariate distribution of β_0 and of β_1 .

Presented new t-statistics of β_0 and of β_1 .

Presented way to bivariate threshold on β_0 and of β_1 .



Thank You

Questions?