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Marquette University



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# Department of Mathematical and Statistical Sciences Marquette University

Syllabus Spring 2024

Course: MSSC 6020 Statistical Simulation

**Time:** TuTh 5:00 pm - 6:15 pm

Location: Cudahy 137 (in-person)

Office Hours: TuTh 4:00 pm - 5:00 Cudahy 313 & by arrangement.

Instructor: Daniel B. Rowe, Ph.D. daniel.rowe@marquette.edu



Course Description From The University Bulletin

#### MSSC 6020. Statistical Simulation. 3 cr. hrs.

Elements of statistical simulation and modeling with applications. Generation of random variables, simulating statistical models, Monte Carlo method, Markov chains, birth-and-death processes, queues, variance reduction, Markov chain Monte Carlo (MCMC) methods and applications, bootstrapping, validation and analysis of simulated data. Prereq: MSSC 6010 and programming competency in a high-level language.

I am not the prerequisite enforcer!



Office Hours: TuTh 4:00-5:00 pm & by arrangement

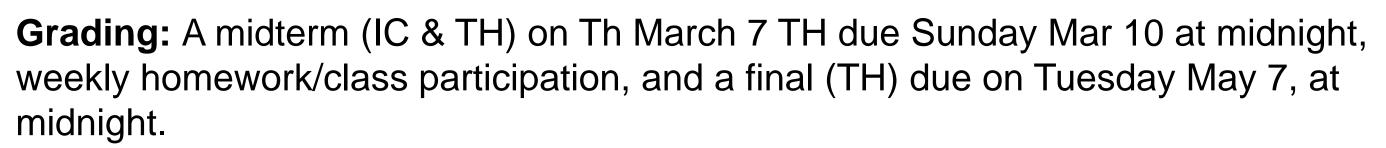
Office: Cudahy Hall 313

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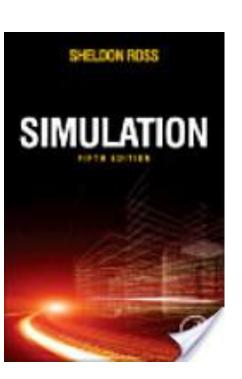
Text: Ross, Sheldon. (2012).

Simulation, Fifth edition, Academic Press.

ISBN: 0124159710



Homework/Participation (30%), Midterm (30%), Final (40%).





### **Chapter 2: Elements of Probability**

Covered by prerequisite.

Sample Space and Events, Axioms of Probability, Random Variables, Expectation, Discrete RVs, Continuous RVs, Conditional Expectation and Variance

### **Numerical Integration**

#### **Chapter 3: Random Numbers**

Number Generation, Random Numbers to Evaluate Integrals

### **Chapter 4: Generating Discrete RVs**

Inverse Transform, Poisson RV, Binomial RV, Acceptance-Rejection, Composition Approach, Alias Method, Random Vectors



#### **Transformation of Variables**

Continuous Distributions, PDF, CDF, Transformation of Variable, Uniform, Normal Distribution

### **Chapter 5: Generating Continuous RVs**

Inverse Transform, Rejection Polar Method for Normal RVs, Poisson Processes, Nonhomogeneous Poisson Processes, 2D Poisson Process.

#### **Bivariate Transformation of Variables**



**Chapter 6: Multivariate Normal and Copulas** 

Multivariate Normal, Generating Multivariate Normal RVs, Copulas,

**Generating Variables from Copula Models** 

**Wishart Distribution** 

Line Fitting and Univariate Multiple Regression

**Multivariate Multiple Regression** 



### **Chapter 7: Discrete Event Simulation**

Discrete Events, Queueing Systems, Inventory Model, Insurance Risk Model, Repair Problem, Stock Option

### **Chapter 8: Analysis of Simulated Data**

Sample Mean and Variance, Interval Estimates of Mean, Bootstrapping for Mean Square Error

#### **Chapter 9: Variance Reduction Techniques**

Antithetic Variables, Control Variates, Variance Reduction by Conditioning, Stratified Sampling, Importance Sampling, Common Random Numbers, Exotic Option

#### **Confidence Intervals for Variance**



#### The Correlation Coefficient

### **Bayesian Statistics**

#### **Chapter 10: Additional Variance Reduction Techniques**

Conditional Bernoulli Sampling, Normalized Importance Sampling,

Latin Hyper Cube Sampling

### **Chapter 11: Statistical Validation Techniques**

Goodness of Fit Tests, Two Sample Problem, Validating Assumptions of a Nonhomogeneous Poisson Process

### **Chapter 12: Markov Chain Monte Carlo Methods**

Markov Chains, Hastings-Metropolis Algorithm, Gibbs Sampler, Markov Chains and Queueing Loss, Simulated Annealing, Sampling Importance Resampling



**Numerical Flavor** 

All slides are a summary of the material and do not contain all detail. Book is ultimate authority.

Familiarize yourself with Matlab.



# Questions?