# MATH 4740/MSSC 5740 Chapter 10 Problem Solving # \* (sign test), 5 (Mann-Whitney U Test)

## 10.5 Summary

Sign Test: <i>MD</i> = <i>MD</i> <sub>0</sub>	$x =$ number of observations > $MD_0$
(One Sample)	If value< $MD_0$ , If value= $MD_0$ , 0. If value> $MD_0$ , +.
Mann-Whitney U Test: Two populations equal or not (not-Paired)	$U_{1} = n_{1}n_{2} + \frac{n_{1}(n_{1}+1)}{2} - R_{1}$ $U_{2} = n_{1}n_{2} + \frac{n_{2}(n_{2}+1)}{2} - R_{2}$ $U = \min(U_{1}, U_{2})$

# Sign Test Table (Table 6)

Two-Sided Test $\alpha$	.10	.05	.02	.01
One-Sided Test $\alpha$	.05	.025	.01	.005
п				
1				
2				
3				
4				
5	0			
6	0	0		
7	0	0	0	
8	1	0	0	0
9	1	1	0	0
10	1	1	0	0
11	2	1	1	0
12	2	2	1	1
13	3	2	1	1
14	3	2	2	1
15	3	3	2	2
16	4	3	2	2
17	4	4	3	2
18	5	4	3	3
19	5	4	4	3
20	5	5	4	3
21	6	5	4	4
22	6	5	5	4
23	7	6	5	4
24	7	6	5	5
25	7	7	6	5

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## Mann-Whitney U Test Table (Table 7)

wo-	Sided	lest	$\alpha =$	0.05																
										n	1									
n <sub>2</sub>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
2								0	0	0	0	1	1	1	1	1	2	2	2	2
3					0	1	1	2	2	3	3	4	4	5	5	6	6	7	7	8
4				0	1	2	3	4	4	5	6	7	8	9	10	11	11	12	13	13
5			0	1	2	3	5	6	7	8	9	11	12	13	14	15	17	18	19	20
6			1	2	3	5	6	8	10	11	13	14	16	17	19	21	22	24	25	2
7			1	3	5	6	8	10	12	14	16	18	20	22	24	26	28	30	32	34
8		0	2	4	6	8	10	13	15	17	19	22	24	26	29	31	34	36	38	4
9		0	2	4	7	10	12	15	17	20	23	26	28	31	34	37	39	42	45	4
10		0	3	5	8	11	14	17	20	23	26	29	33	36	39	42	45	48	52	5
11		0	3	6	9	13	16	19	23	26	30	33	37	40	44	47	51	55	58	6
12		1	4	7	11	14	18	22	26	29	33	37	41	45	49	53	57	61	65	6
13		1	4	8	12	16	20	24	28	33	37	41	45	50	54	59	63	67	72	70
4		1	5	9	13	17	22	26	31	36	40	45	50	55	59	64	67	74	78	8
15		1	5	10	14	19	24	29	34	39	44	49	54	59	64	70	75	80	85	91
16		1	6	11	15	21	26	31	37	42	47	53	59	64	70	75	81	86	92	98
17		2	6	11	17	22	28	34	39	45	51	57	63	67	75	81	87	93	99	10
18		2	7	12	18	24	30	36	42	48	55	61	67	74	80	86	93	99	106	112
9		2	7	13	19	25	32	38	45	52	58	65	72	78	85	92	99	106	113	11
20		2	8	13	20	27	34	41	48	55	62	69	76	83	90	98	105	112	119	12

#### One-Sided Test $\alpha = 0.05$

										n	1									
n <sub>2</sub>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
2					0	0	0	1	1	1	1	2	2	2	3	3	3	4	4	4
3			0	0	1	2	2	3	3	4	5	5	6	7	7	8	9	9	10	11
4			0	1	2	3	4	5	6	7	8	9	10	11	12	14	15	16	17	18
5		0	1	2	4	5	6	8	9	11	12	13	15	16	18	19	20	22	23	25
6		0	2	3	5	7	8	10	12	14	16	17	19	21	23	25	26	28	30	32
7		0	2	4	6	8	11	13	15	17	19	21	24	26	28	30	33	35	37	39
8		1	3	5	8	10	13	15	18	20	23	26	28	31	33	36	39	41	44	47
9		1	3	6	9	12	15	18	21	24	27	30	33	36	39	42	45	48	51	54
10		1	4	7	11	14	17	20	24	27	31	34	37	41	44	48	51	55	58	62
11		1	5	8	12	16	19	23	27	31	34	38	42	46	50	54	57	61	65	69
12		2	5	9	13	17	21	26	30	34	38	42	47	51	55	60	64	68	72	77
13		2	6	10	15	19	24	28	33	37	42	47	51	56	61	65	70	75	80	84
14		2	7	11	16	21	26	31	36	41	46	51	56	61	66	71	77	82	87	92
15		3	7	12	18	23	28	33	39	44	50	55	61	66	72	77	83	88	94	100
16		3	8	14	19	25	30	36	42	48	54	60	65	71	77	83	89	95	101	107
17		3	9	15	20	26	33	39	45	51	57	64	70	77	83	89	96	102	109	115
18		4	9	16	22	28	35	41	48	55	61	68	75	82	88	95	102	109	116	123
19	0	4	10	17	23	30	37	44	51	58	65	72	80	87	94	101	109	116	123	130
20	0	4	11	18	25	32	39	47	54	62	69	77	84	92	100	107	115	123	130	138

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### **10.6 Practice Problems**

\* A group of n=15 students was surveyed about the number of times they've unlocked their phone yesterday. Unlocks: 12 13 19 20 21 21 23 23 24 25 28 29 34 38 47 Their statistics professor claims students unlock their phone more than 20 times per day. Go through the 5 hypothesis testing steps to test whether the median number is greater than 20.  $\alpha=0.05$ 

**Step 1**. Set up hypotheses and determine level of significance.

H<sub>0</sub>: MD=20 vs. H<sub>1</sub>: MD>20  $\alpha = 0.05$ 

**Step 2**. Select the appropriate test statistic.

 $x = (\text{the number of observations} > MD_0)$ 

	et up deci t H <sub>0</sub> if <i>P</i> (.		
x	P(X=x)	P(X≤x)	P(X≥x)
0	0.0000	0.0000	1.0000
1	0.0005	0.0005	1.0000
2	0.0032	0.0037	0.9995
3	0.0139	0.0176	0.9963
4	0.0417	0.0592	0.9824
5	0.0916	0.1509	0.9408
6	0.1527	0.3036	0.8491
7	0.1964	0.5000	0.6964
8	0.1964	0.6964	0.5000
9	0.1527	0.8491	0.3036
10	0.0916	0.9408	0.1509
11	0.0417	0.9824	0.0592
12	0.0139	0.9963	0.0176
13	0.0032	0.9995	0.0037
14	0.0005	1.0000	0.0005
15	0.0000	1.0000	0.0000
0.2 0.18 0.16 0.14 0.12 0.11 0.08 0.06 0.04 0.02			
Rejec	t H <sub>0</sub> if $x \ge 1$		10 11 12 13 14

Use binomial probabilities n=5, p=1/2.

Sorted	Signs>20	Ranks
12	-1	1
13	-1	2
19	-1	3
20	0	4
21	+1	5
21	+1	6
23	+1	7
23	+1	8
24	+1	9
25	+1	10
28	+1	11
29	+1	12
34	+1	13
38	+1	14
47	+1	15

## Step 5. Conclusion.

We do not reject H<sub>0</sub> because 11 < 12. We do not have statistically significant evidence at  $\alpha$  = 0.05 to show that the statistics students look at their phone more than 20 times per day. Compare to *t*? Note:  $\overline{X}$  =24.933, *s* =9.0512, *t*=2.1713, *t*<sub>0.05,14</sub>=1.761

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**5.** The recommended daily allowance of Vitamin A for children between 1 and 3 years of age is 400 micrograms (mcg). Vitamin A deficiency is linked to a number of adverse health outcomes, including poor eyesight, susceptibility to infection, and dry skin. The following are Vitamin A concentrations in children with and without poor eyesight, a history of infection, and dry skin.

 With:
 120
 420
 180
 345
 390
 430
 (Group 1)

 Without:
 450
 500
 395
 380
 430
 (Group 2)

Is there a significant difference in Vitamin A concentrations between children with and without poor eyesight, a history of infection, and dry skin? Run the appropriate test at a 5% level of significance.

**Step 1**. Set up hypotheses and determine level of significance.

H<sub>0</sub>: The two populations are equal

vs.

H<sub>1</sub>: The two populations are not equal.  $\alpha = 0.05$ 

Step 2. Select the appropriate test statistic.

 $U = \min(U_1, U_2), \qquad U_1 = n_1 n_2 + \frac{n_1(n_1 + 1)}{2} - R_1, \qquad U_2 = n_1 n_2 + \frac{n_2(n_2 + 1)}{2} - R_2$ Step 3. Set up decision rule. Reject H<sub>0</sub> if  $U < U_{\alpha, n_1, n_2} = U_{0.05, 6, 5} = 3$ . Step 4. Compute the test statistic.

Tota	l Sample	Ranks					
With	Without	With	Without				
120		1					
180		2					
345		3					
	380		4				
390		5					
	395		6				
420		7					
430	430	8.5	8.5				
	450		10				
	500		11				
		R <sub>1</sub> =26.5	R <sub>2</sub> =39.5				

 $U_1 = (6)(5) + \frac{6(6+1)}{2} - 26.5 = 24.5$  $U_2 = (6)(5) + \frac{5(5+1)}{2} - 39.5 = 5.5$  $U = \min(24.5, 5.5) = 5.5$ 

### Step 5. Conclusion.

Because  $U=5.5 \ge U_{0.05,6,5}=3$ , fail to reject H<sub>0</sub>. No evidence to show there is a significant difference in Vitamin A concentrations between children with and without poor eyesight, a history of infection, and dry skin.