MATH 1700

Class 24

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Be The Difference.

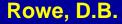
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Agenda:

Recap Chapter 10.4-10.5

Lecture Chapter 11.1-11.3

Recap Chapter 10.4-10.5



10: Inferences Involving Two Populations 10.4 Inference for Difference between Two Proportions

Interested in comparisons between proportions $p_1 - p_2$.

If independent samples of size n_1 and n_2 are drawn ... with $p_1=P_1$ (success) and $p_2=P_2$ (success), then the sampling distribution of $p'_1 - p'_2$ has these properties:

1. mean
$$\mu_{p_1'-p_2'} = p_1 - p_2$$

2. standard error $\sigma_{p_1'-p_2'} = \sqrt{\frac{p_1q_1}{n_1} + \frac{p_2q_2}{n_2}}$ (10.10)

3. approximately normal dist if n_1 and n_2 are sufficiently large. ie I $n_1, n_2 > 20$ II $n_1p_1, n_1q_1, n_2p_2, n_2q_2 > 5$ III sample<10% of pop

10: Inferences Involving Two Populations 10.4 Inference for Difference between Two Proportions Confidence Interval Procedure

Assumptions for ... difference between two proportions p_1-p_2 : The n_1 ... and n_2 random observations ... are selected independently from two populations that are not changing

Confidence Interval for the Difference between Two Proportions $p_1 \cdot p_2$

$$(p_{1}'-p_{2}')-z(\alpha/2)\sqrt{\frac{p_{1}'q_{1}'}{n_{1}}+\frac{p_{2}'q_{2}'}{n_{2}}} \text{ to } (p_{1}'-p_{2}')+z(\alpha/2)\sqrt{\frac{p_{1}'q_{1}'}{n_{1}}+\frac{p_{2}'q_{2}'}{n_{2}}}$$

where $p_{1}'=\frac{x_{1}}{n_{1}}$ and $p_{2}'=\frac{x_{2}}{n_{2}}$. (10.11)

10: Inferences Involving Two Populations 10.4 Inference for Difference between Two Proportions Confidence Interval Procedure

Example: a = 0.01Construct a 99% CI for proportion of female *A*'s minus male *A*'s difference $p_f - p_m$.

120 values
$$z(\alpha/2) = 2.58$$
 $(p'_f - p'_m) \pm z(\alpha/2) \sqrt{\frac{p'_f q'_f}{n_f} + \frac{p'_m q'_m}{n_m}}{\frac{n_m}{n_m}}$
 $n_m = 52$
 $n_f = 68$ $p'_f = \frac{x_f}{n_f} = \frac{43}{68} = .62$ $(.62 - .40) \pm 2.58 \sqrt{\frac{(.62)(.38)}{68} + \frac{(.40)(.60)}{52}}{52}}$
 $x_m = 21$ $p'_m = \frac{x_m}{n_m} = \frac{21}{52} = .40$ -.003 to .460

10: Inferences Involving Two Populations 10.4 Inference for Difference between Two Proportions Hypothesis Testing Procedure

We can perform hypothesis tests on the proportion $\frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2} = pq \left| \frac{1}{n_1} + \frac{1}{n_2} \right|$ $H_0: p_1 \ge p_2$ vs. $H_a: p_1 < p_2$ $H_0: p_1 \le p_2$ VS. $H_a: p_1 > p_2$ when $p_1 = p_2 = p_1$. $H_0: p_1 = p_2$ VS. $H_a: p_1 \neq p_2$ Test Statistic for the Difference between two Proportions $z^{*} = \frac{(p_{1}' - p_{2}') - (p_{0,1} - p_{0,2})}{\sqrt{pq\left[\frac{1}{n_{1}} + \frac{1}{n_{2}}\right]}} \quad Population$ Population Proportions Known (10.12)7 Rowe, D.B. *p* known

10: Inferences Involving Two Populations 10.4 Inference for Difference between Two Proportions Hypothesis Testing Procedure

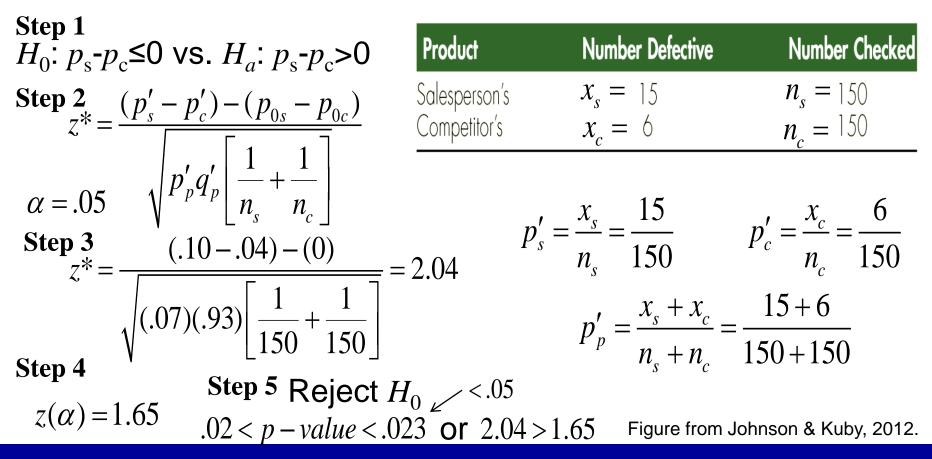
Test Statistic for the Difference between two Proportions-Population Proportions **UnKnown** $z^* = \frac{(p'_1 - p'_2) - (p_{0,1} - p_{0,2})}{\sqrt{p'_p q'_p \left[\frac{1}{n_1} + \frac{1}{n_2}\right]}}$ (10)

where we assume $p_1 = p_2$ and use pooled estimate of proportion

$$p_1' = \frac{x_1}{n_1} \quad p_2' = \frac{x_2}{n_2} \qquad \frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2} = pq \left[\frac{1}{n_1} + \frac{1}{n_2}\right] \qquad \downarrow \qquad p_p' = \frac{x_1 + x_2}{n_1 + n_2}$$

10: Inferences Involving Two Populations 10.4 Inference for Difference between Two Proportions

Is proportion of Salesman's defectives less than Competitor's? $\alpha = .05$



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10: Inferences Involving Two Populations 10.5 Inference for Ratio of Two Variances Two Ind. Samples Hypothesis Testing Procedure

We can perform hypothesis tests on two variances

 $H_0: \sigma_1^2 \ge \sigma_2^2 \text{ vs. } H_a: \sigma_1^2 < \sigma_2^2$ $H_0: \sigma_1^2 \le \sigma_2^2 \text{ vs. } H_a: \sigma_1^2 > \sigma_2^2$ $H_0: \sigma_1^2 = \sigma_2^2 \text{ vs. } H_a: \sigma_1^2 \neq \sigma_2^2$

Assumptions: Independent samples from normal distribution

Test Statistic for Equality of Variances

$$S^* = \frac{S_n^2}{S_d^2}$$

with
$$df_n = n_n - 1$$
 and $df_d = n_d - 1$.

(10.16)

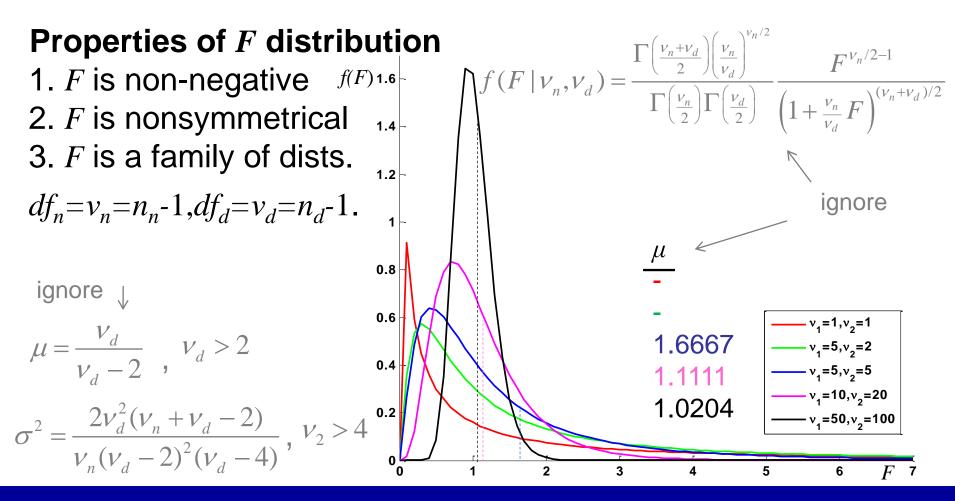
Actually ← ignore

 $F^{*} = \frac{\left[(n_{n} - 1)s_{n}^{2} / \sigma^{2} \right] / (n_{n} - 1)}{\left[(n_{d} - 1)s_{d}^{2} / \sigma^{2} \right] / (n_{d} - 1)}$

Use new table to find areas for new statistic.

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10: Inferences Involving Two Populations 10.5 Inference for Ratio of Two Variances Two Ind. Samples



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10: Inferences Involving Two Populations 10.5 Inference for Ratio of Two Variances Two Ind. Samples Hypothesis Testing Procedure

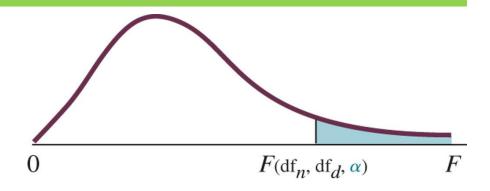
Test Statistic for Equality of Variances

with
$$df_n = n_n - 1$$
 and $df_d = n_d - 1$. (10.16)

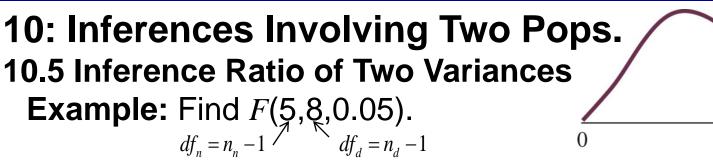
Will also need critical values. $P(F > F(df_n, df_d, \alpha)) = \alpha$

Table 9 Appendix B Page 722

 $F^* = \frac{S_n^2}{S_d^2}$







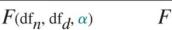


Table 9, Appendix B, Page 722.

Degrees of Freedom for Numerator df_n

	<i></i>	00		U				on			
d L		1	2	3	4	5	6	7	8	9	10
for Denominator df_d	1 2 3 4 5	161. 18.5 10.1 7.71 6.61	200. 19.0 9.55 6.94 5.79	216. 19.2 9.28 6.59 5.41	225. 19.2 9.12 6.39 5.19	230. 19.3 9.01 6.26 5.05	234. 19.3 8.94 6.16 4.95	237. 19.4 8.89 6.09 4.88	239. 19.4 8.85 6.04 4.82	241. 19.4 8.81 6.00 4.77	242. 19.4 8.79 5.96 4.74
Degrees of Freedom	6 7 8 9 10	5.99 5.59 5.32 5.12 4.96	5.14 4.74 4.46 4.26 4.10	4.76 4.35 4.07 3.86 3.71	4.53 4.12 3.84 3.63 3.48	4.39 3.97 3.69 3.48 3.33	4.28 3.87 3.58 3.37 3.22	4.21 3.79 3.50 3.29 3.14	4.15 3.73 3.44 3.23 3.07	4.10 3.68 3.39 3.18 3.02	4.06 3.64 3.35 3.14 2.98
	The second second	1						Eiguro	c from Joh	ncon & Kul	2012

Figures from Johnson & Kuby, 2012.

 $\alpha = 0.05$

10: Inferences Involving Two Populations 10.5 Inference for Ratio of Two Variances Two Ind. Samples Hypothesis Testing Procedure

One tailed tests: Arrange H_0 & H_a so H_a is always "greater than" $H_0: \sigma_1^2 \ge \sigma_2^2$ VS. $H_a: \sigma_1^2 < \sigma_2^2 \rightarrow H_0: \sigma_2^2 / \sigma_1^2 \le 1$ VS. $H_a: \sigma_2^2 / \sigma_1^2 > 1$ $F^* = \frac{s_2^2}{s_v^2}$ $H_0: \sigma_1^2 \le \sigma_2^2$ VS. $H_a: \sigma_1^2 > \sigma_2^2 \rightarrow H_0: \sigma_1^2 / \sigma_2^2 \le 1$ VS. $H_a: \sigma_1^2 / \sigma_2^2 > 1$ $F^* = \frac{s_1^2}{s_2^2}$ Reject H_0 if $F^* = s_n^2 / s_d^2 > F(df_n, df_d, \alpha)$.

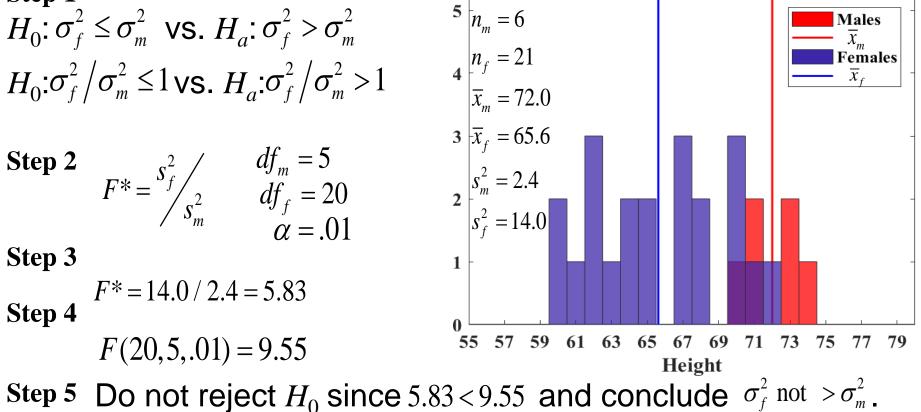
Two tailed tests: put larger sample variance s^2 in numerator $H_0: \sigma_1^2 = \sigma_2^2$ vs. $H_a: \sigma_1^2 \neq \sigma_2^2 \rightarrow H_0: \sigma_n^2 / \sigma_d^2 = 1$ vs. $H_a: \sigma_n^2 / \sigma_d^2 \neq 1$ $\sigma_n^2 = \sigma_1^2$ if $s_1^2 > s_2^2$, $\sigma_n^2 = \sigma_2^2$ if $s_2^2 > s_1^2$

Reject H_0 if $F^* = s_n^2 / s_d^2 > F(df_n, df_d, \alpha/2)$.

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10: Inferences Involving Two Populations 10.5 Inference for Ratio of Two Variances Two Ind. Samples

Is variance of female heights greater than that of males? $\alpha = .01$ 27 values Step 1

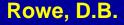


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Chapter 10: Inferences Involving Two Populations

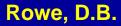
Questions?

Homework: Read Chapter 10.4-10.5 WebAssign Chapter 10# 83, 85, 91, 98, 99, 101, 111, 113, 115, 117, 119, 125, 133





Lecture Chapter 11.1-11.3



Chapter 11: Applications of Chi-Square

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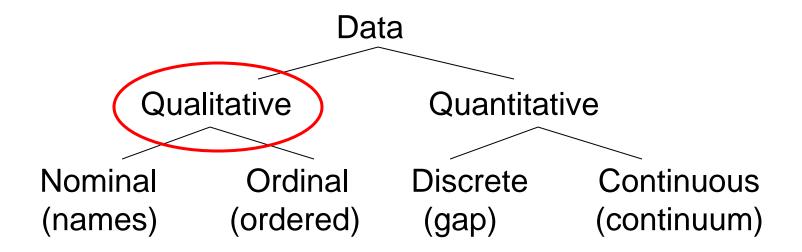
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Marquette University Recall

1: Statistics 1.2 What is Statistics?

Data: The set of values collected from the variable from each of the elements that belong to the sample.



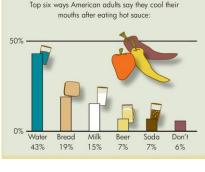
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11: Applications of Chi-Square 11.1 Chi-Square Statistic Cooling a Great Hot Taste

Quite often we have qualitative data in categories.

Example: Cooling mouth after hot spicy food.

Method	Water	Bread	Milk	Beer	Soda	Nothing	Other
Number	73	29	35	19	20	13	11



Putting Out The Fire

11: Applications of Chi-Square 11.1 Chi-Square Statistic Data Setup

Example: Cooling mouth after hot spicy food.

Method	Water	Bread	Milk	Beer	Soda	Nothing	Other	
Number	73	29	35	19	20	13	11	

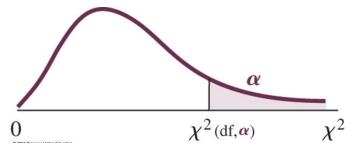
Data set up: *k* cells C_1, \ldots, C_k that *n* observations sorted into Observed frequencies in each cell O_1, \ldots, O_k . $O_1 + \ldots + O_k = n$ Expected frequencies in each cell E_1, \ldots, E_k . $E_1 + \ldots + E_k = n$

Cell	C_1	<i>C</i> ₂	-	C_k
Observed	<i>O</i> ₁	<i>O</i> ₂		O_k
Expected	E_1	E_2		E_k

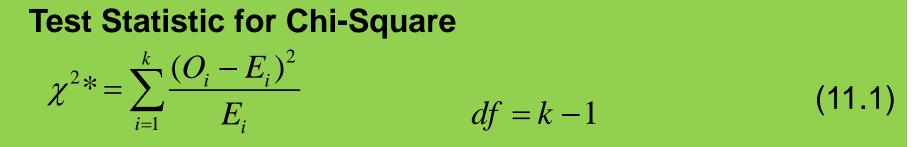


11: Applications of Chi-Square 11.1 Chi-Square Statistic

Outline of Test Procedure



When we have observed cell frequencies O_1, \ldots, O_k , we can test to see if they match with some expected cell frequencies E_1, \ldots, E_k .



If the O_i 's are different from E_i 's then χ^{2*} is "large." Go through 5 hypothesis testing steps as before.

11: Applications of Chi-Square 11.1 Chi-Square Statistic

Assumption for using the chi-square statistic to make inferences based upon enumerative data: ... a random sample drawn from a population where each individual is classified according to the categories

$$\chi^{2} * = \sum_{i=1}^{k} \frac{(O_{i} - E_{i})^{2}}{E_{i}} \qquad df = k - 1$$

observed cell frequencies O_1, \ldots, O_k , expected cell frequencies E_1, \ldots, E_k .

11: Applications of Chi-Square 11.2 Inferences Concerning Multinomial Experiments

Example: We work for Las Vegas Gaming Commission. We have received many complaints that dice at particular casino are loaded (weighted, not fair). We confiscate all dice and test one. We roll it n=60 times. We get following data.

Cell, <i>i</i>	1	2	3	4	5	6
Observed, O_i	7	12	10	12	8	11
Expected, E_i	10	10	10	10	10	10

Expected Value for Multinomial Experiment:

$$E_i = np_i \tag{11.3}$$



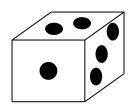
11: Applications of Chi-Square

11.2 Inferences Concerning Multinomial Experiments

Example: We roll it *n*=60 times. We get following data.

Cell, i	1	2	3	4	5	6
Observed, O_i	7	12	10	12	8	11
Expected, E_i	10	10	10	10	10	10
$E_i = 60(1/6)$						

Is the die fair? Need to go through the hypothesis testing procedure to determine if it is fair.



11: Applications of Chi-Square 11.2 Inferences Concerning Multinomial Experiments

Exampl Calculatin	e: Is the die faig χ^2	air? $\chi^{2*} = \sum_{i=1}^{k} \frac{1}{2}$	$\frac{(O_i - E_i)^2}{E_i}$		F for Mult: (11.2)
Number	Observed (O)	Expected (E)	0 – E	(O – E) ²	$rac{(O-E)^2}{E}$
1 2 3 4 5 6	7 12 10 12 8 11	10 10 10 10 10 10	-3 2 0 2 -2 1	9 4 0 4 4 1	0.9 0.4 0.0 0.4 0.4 0.1
Total	60	60	0 (ck)		$\chi^{2*} = 2.2$
	<i>O</i> ₁ ++ <i>O</i> _k = <i>n</i>	$E_1 + + E_k = n$	Fig	ure from Johnso	on & Kuby, 2012.

11: Applications of Chi-Square

11.2 Inference for Mean Difference Two Dependent Samples

Cell	1	2	3	4	5	6
Observed	7	12	10	12	8	11
Expected	10	10	10	10	10	10

Observed different than expected? Step 1 Fill in.

Step 2

Step 3Step 4

Step 5

 χ^2 Figures from Johnson & Kuby, 2012.



 χ^2

k = 6

11: Applications of Chi-Square

11.2 Inference for Mean Difference Two Dependent Samples

Cell	1	2	3	4	5	6	
Observed	7	12	10	12	8	11	
Expected	10	10	10	10	10	10	

Observed different than expected? Step 1 H_0 : Die fair p_i 's = $\frac{1}{6}$ H_a : Die not fair p_i 's $\neq \frac{1}{6}$ Step 2

Step 3 Step 4

Step 5



k = 6

11: Applications of Chi-Square

11.2 Inference for Mean Difference Two Dependent Samples

Cell	1	2	3	4	5	6	
Observed	7	12	10	12	8	11	
Expected	10	10	10	10	10	10	

Observed different than expected? Step 1 H_0 : Die fair p_i 's = $\frac{1}{6}$ H_a : Die not fair p_i 's $\neq \frac{1}{6}$ Step 2 $\chi^{2*} = \sum_{i=1}^{k} \frac{(O_i - E_i)^2}{E_i}$ df = k - 1 $\alpha = .05$ Step 3 Step 4

Step 5

k = 6

11: Applications of Chi-Square

11.2 Inference for Mean Difference Two Dependent Samples

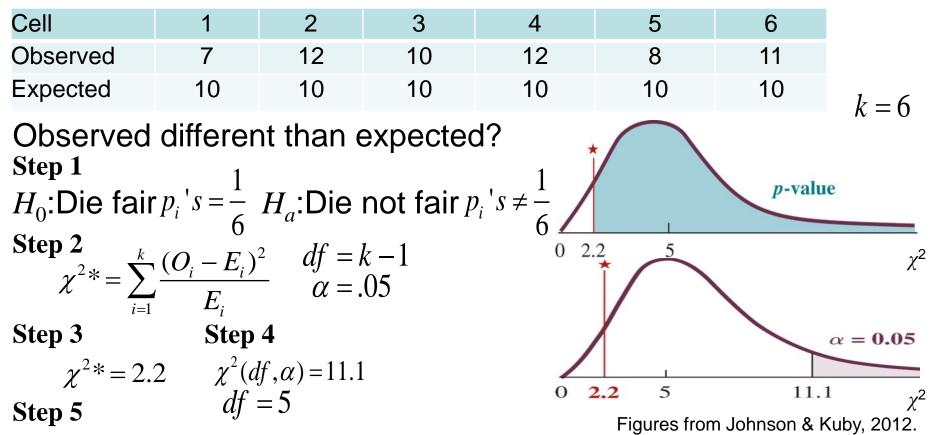
Cell	1	2	3	4	5	6	
Observed	7	12	10	12	8	11	
Expected	10	10	10	10	10	10	

Observed different than expected? Step 1 H_0 : Die fair p_i 's = $\frac{1}{6}$ H_a : Die not fair p_i 's $\neq \frac{1}{6}$ Step 2 $\chi^{2*} = \sum_{i=1}^{k} \frac{(O_i - E_i)^2}{E_i}$ df = k - 1 $\alpha = .05$ Step 3 $\chi^{2*} = 2.2$

Step 5

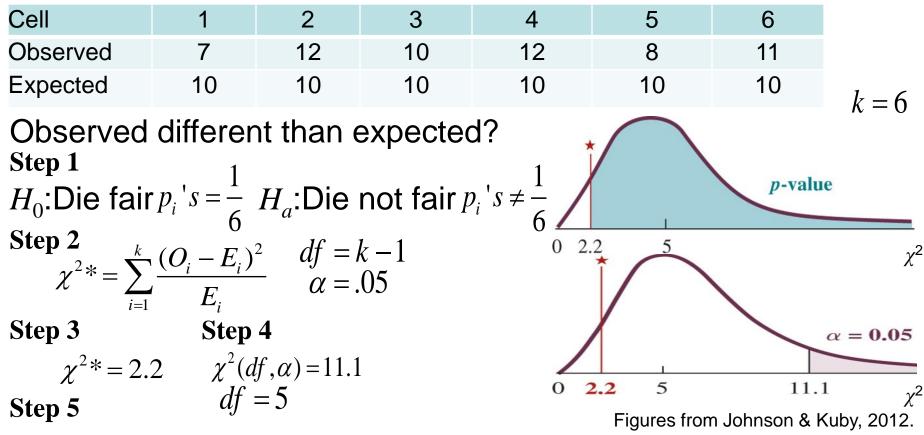
11: Applications of Chi-Square

11.2 Inference for Mean Difference Two Dependent Samples



11: Applications of Chi-Square

11.2 Inference for Mean Difference Two Dependent Samples



Since .05<*p*-value=.82 or because $\chi^2 * < \chi^2(df, \alpha)$, fail to reject H_0

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Marquette University Recall

3: Descriptive Analysis and Bivariate Data

3.1 Bivariate Data

Bivariate data: The values of two different variables that are obtained from the same population element.

Qualitative-Qualitative Qualitative-Quantitative Quantitative-Quantitative

When Qualitative-Qualitative **Cross-tabulation tables** or **contingency tables** Sometimes called r by c ($r \times c$)

Marquette University Recall

3: Descriptive Analysis and Bivariate Data

3.1 Bivariate Data: two qualitative

Example: Construct a 2×3 table.

Name	Gender	Major	Name	Gender	Major	Name	Gender	Major
Adams	M	LA	Feeney	Μ	Т	McGowan	M	BA
Argento	F	BA	Flanigan	\sim	LA	Mowers	F	BA
Baker	M	LA	Hodge	F	LA	Ornt	\sim	Т
Bennett	F	LA	Holmes	\sim	Т	Palmer	F	LA
Brand	M	Т	Jopson	F	Т	Pullen	M	Т
Brock	M	BA	Kee	\sim	BA	Rattan	\sim	BA
Chun	F	LA	Kleeberg	M	LA	Sherman	F	LA
Crain	M	Т	Light	M	BA	Small	F	Т
Cross	F	BA	Linton	F	LA	Tate	M	BA
Ellis	F	BA	lopez	M	Т	Yamamoto	M	LA

	Major		
Gender	LA	BA	Т
M F	(5) (6)	(6) (4)	(7) (2)

M = male F = female LA = liberal arts BA = business adminT = technology

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables

Example:

Construct a 2×3 table.

Each in group of 300 students identified as male or female and asked if preferred classes in math-science, social science, or humanities.

Sample Results for Gender and Subject Preference

		Favorite Subject Area		
Gender	Math–Science (MS)	Social Science (SS)	Humanities (H)	Total
Male (M) Female (F)	37 35	41 72	44 71	122 178
Total	72	113	115	300

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Independence*

Is "Preference for math-science, social science, or humanities" ... "independent of the gender of a college student?"

Sample Results for Gender and Subject Preference

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11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Independence*

Is "Preference for math-science, social science, or humanities" ... "independent of the gender of a college student?"

There is a Hypothesis test (of independence) to determine this. Is Favorite Subject independent of Gender.

Similar to Example with the Die, now have rows i and columns j. Observed values, O_{ii} 's.

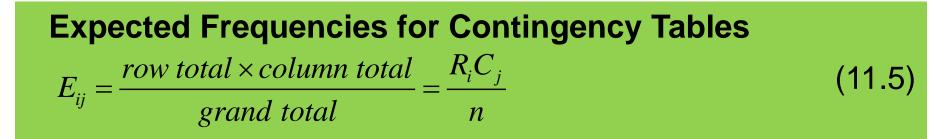
$(\mathbf{O} \mathbf{E})^2$		ij			
$\chi^{2}*-\sum \frac{(O_{ij}-E_{ij})}{(O_{ij}-E_{ij})}$			Favorite Subject Area		
	Gender	Math–Science (MS)	Social Science (SS)	Humanities (H)	Total
all cells E_{ij}	Male (M) Female (F)	37 35	41 72	44 71	122 178
What are E_{ii} 's?	Total	72	113	115	122 178 300
vvnat are <i>L</i> _{ij} S:			Figure from .	Johnson & Kuby,	2012.

(11.4)

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables $\chi^{2*} = \sum_{all \ cells} \frac{(O_{ij} - E_{ij})^2}{E_{ij}}$

D of **F** for Contingency Tables: df = (r-1)(c-1)

r>1,*c*>1



Where does this formula for E_{ii} 's come from?

rows *i* and columns *j*

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Marquette University Recall

4: Probability

4.5 Independent Events

Independent events: Two events are independent if the occurrence or nonoccurence of one gives us no information about the likeliness of occurrence for the other.

In algebra: P(A) = P(A | B) = P(A | not B)

In words:

1. Prob of *A* unaffected by knowledge that *B* has occurred, not occurred, or no knowledge.

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4: Probability 4.5 Independent Events

Two events *A* and *B* are independent if the probability of one is not "influenced" by the occurrence or nonoccurrence of the other.

Two Events A and B are independent if:

- 1. P(A) = P(A | B)
- 2. P(B) = P(B|A)
- 3. $P(A \text{ and } B) = P(A) \cdot P(B)$

Examples:?

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Independence*

$$E_{ij} = \frac{R_i C_j}{n}$$

Where does this formula for E_{ij} 's come from?

	Favorite Subject Area			
Gender	Math–Science (MS)	Social Science (SS)	Humanities (H)	Total
Male (M) Female (F)	37 35	41 72	44 71	122 178
Total	72	113	115	300

If Favorite Subject (column variable) is independent of Gender (row variable), then

$$P(MS \mid M) = P(MS \mid F) = P(MS)$$

P(A) = P(A | B) $P(A \text{ and } B) = P(A) \cdot P(B)$

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Independence*

$$E_{ij} = \frac{R_i C_j}{n}$$

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Where does this formula for E_{ij} 's come from?

	MS	SS	Н	Total
Male Female	29.28 42.72	45.95 67.05	46.77 68.23	122.00 178.00
Total	72.00	113.00	115.00	300.00

$$P(M) = 122 / 300$$

 $P(F) = 178 / 300$

P(MS) = 72 / 300

P(SS) = 113 / 300

P(H) = 115 / 300

If Favorite Subject is independent of Gender, then

P(M and MS) = P(M)P(MS) = (122 / 300)(72 / 300)

E(M and MS) = nP(M)P(MS) = 300(122/300)(72/300)

 $E(M \text{ and } MS) = 122 \times 72 / 300$

Figure from Johnson & Kuby, 2012.

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MS

37 (29.28)

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Independence*

$$E_{ij} = \frac{R_i C_j}{n}$$

Where does this formula for E_{ij} 's come from? Favorite Subject Area

SS

Female	35 (42.72)	72 (67.05)	71 (68.23)	178	c=3
Total	72	113	115	300	
If Favo	orite Subjec	t is indepe	ndent of Ge	ender, th	ien

41 (45.95) 44 (46.77)

Н

Total

122

$$\chi^{2*} = \sum_{all \ cells} \frac{(O_{ij} - E_{ij})^{2}}{E_{ij}} < \chi^{2}(2,0.05) \qquad \alpha = 0.05$$

$$\chi^{2*} = 4.604 < \chi^{2}(2,0.05) = 5.99$$

Figure from Johnson & Kuby, 2012.

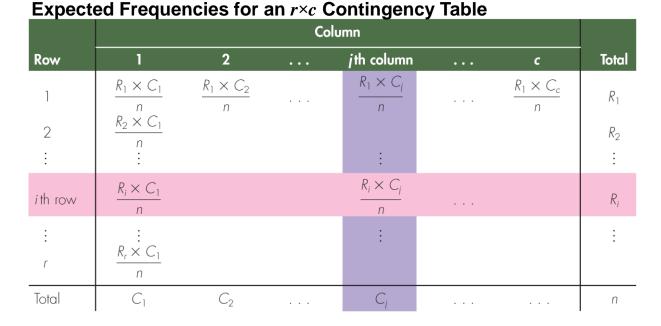
r=2

Rowe, D.B.

Gender

Male

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Independence*



$$\chi^{2} * = \sum_{all \ cells} \frac{(O_{ij} - E_{ij})^{2}}{E_{ij}} < \chi^{2}((r-1)(c-1), \alpha)$$

Figure from Johnson & Kuby, 2012.

Rowe, D.B.

$$E_{ij} = \frac{R_i C_j}{n}$$

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Homogeneity*

Governor's Proposal Residence Total Favor Oppose 200 Urban 143 .57 Suburban 98 102 200 Rural 13 87 100 254 246 500 Total

If so, then P(F and Urban) = P(F)P(U) E(F and Urban) = nP(F)P(U)E(F and Urban) = 500(254 / 500)(200 / 500)

Is the distribution within all rows the same for all rows?

Rowe, D.B.

 $E_{ij} = \frac{R_i C_j}{1}$

r=3

c=2

11: Applications of Chi-Square 11.3 Inferences Concerning Contingency Tables *Test of Homogeneity*

Is the distribution within all rows the same for all rows?

	Governo		
Residence	Favor	Oppose	Total
Urban Suburban Rural	143 98 13	57 102 87	200 200 100
Total	254	246	500

$$\chi^{2} * = \sum_{all \ cells} \frac{(O_{ij} - E_{ij})^{2}}{E_{ij}} < \chi^{2}((r-1)(c-1), \alpha)$$

 $\alpha = 0.05$ df = (r-1)(c-1) = (3-1)(2-1)

 $E_{ij} = \frac{R_i C_j}{n}$

Chapter 11: Applications of Chi-Square

Questions?

Homework: Read Chapter 11 WebAssign Chapter 11 # 3, 5, 11, 15, 21, 49, 53

